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Disentangling goods, labor, and credit market frictions in three European economies[☆]

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HIGHLIGHTS

- We build a flexible model with search frictions in three markets: credit, labor, and goods market. We then apply this model (called CLG) to three different economies: a flexible, finance-driven economy (the UK), an economy with wage moderation (Germany), and finally an economy with structural rigidities (Spain).
- Goods and credit market frictions play a dominant role in entry costs and account for up to 75% to 85% of total entry costs.
- The demand side amplification effects of adverse supply shocks (through income losses of consumers) remains limited to a range of 15% to 25% of the total impact of these supply shocks.
- Finally, the speed of matching in the goods market and in credit market accounts for a small fraction of unemployment: most of the variation in unemployment comes from the speed of matching in the labor market.

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ABSTRACT

We build a flexible model with search frictions in three markets: credit, labor, and goods markets. We then apply this model (called CLG) to three different economies: a flexible, finance-driven economy (the UK), an economy with wage moderation (Germany), and an economy with structural rigidities (Spain). In these three countries, goods and credit market frictions play a dominant role in entry costs and account for 75% to 85% of the total entry costs. In the goods market, adverse supply shocks are amplified through their propagation to the demand side, as they also imply income losses for consumers. This adds up to, at most, an additional 15% to 25% to the impact of the shocks. Finally, the speed of matching in the goods market and the credit market accounts for a small fraction of unemployment: most variation in unemployment comes from the speed of matching in the labor market.

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1. Introduction

This paper develops a model of credit, labor, and goods market frictions introduced in a symmetrical way, with matching functions associating, respectively, financial institutions and “projects,” job seekers and vacancies, and “selling firms” and “customers.” In particular, it

introduces a structure of search in the goods market and its relation to income that facilitates the exposition of the main concepts and, importantly, implies a convenient recursive structure for the model. As a result, solutions in each market are derived sequentially with equilibrium tightness in the goods market determined first. This leads to transparent and closed-form solutions characterizing a labor market equilibrium, extending the canonical search models. This also allows for a transparent calibration to several European economies, determining the role of entry costs in each of the three markets, the respective role of price and wage markups, and finally the role of complementarities between frictions in each market.

We then apply this model (called CLG) to three different economies: a flexible, finance-driven economy (the UK), an economy with wage moderation (Germany), and an economy with structural rigidities (Spain). Our calibration strategy is to match moments on each markets using flows data in the labor market, capacity

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utilization rates for the goods market, and aggregate data from national accounts in the credit market. In these three countries, goods and credit market frictions play a dominant role in entry costs. They account for the largest part of total entry costs (more than 75%). In the goods market, adverse supply shocks are amplified through their propagation to the demand side, as they also imply income losses for consumers. This adds, at most, an additional 15% to 25% to the impact of the shocks. Finally, the speed of matching in the goods market and the credit market accounts for a small fraction of unemployment: most variation in unemployment comes from the speed of matching in the labor market.

Goods market frictions were introduced in the classical search literature with consumers prospecting in the goods market in order to consume (e.g., Diamond, 1971; Diamond, 1982). Diamond (1982) assumed that two consumers were needed to consume indivisible units of goods (the coconuts). Diamond (1971) instead assumed two sides in the market, consumers and sellers. Only consumers searched for different shops. Shops were located in different places. The striking result of Diamond (1971) was that prices would converge to the monopsony price even with infinitely small search costs.

A recent and growing literature has revived these ideas. A similar logic where consumers and sellers are linked through a matching function in the goods market has been introduced in Wasmer (2009), Lehmann and Van der Linden (2010), Bai et al. (2011), Michailat and Saez (2014), Petrosky-Nadeau and Wasmer (2015). In this paper, we encompass these approaches and assume that firms have imperfect access to financial markets, then imperfect access to the labor market, and finally imperfect access to consumers. Consumers themselves face frictions to consume certain goods and must spend time and resources to access these search goods. As long as they are unsuccessful they have excess income, which they spend on a non-frictional good playing the role of a numeraire. This convenient assumption of a numeraire absorbing the excess liquidity when agents do not access the search good is reminiscent of the night-and-day markets in the search and money literature (Lagos and Wright, 2005; Nosal and Rocheteau, 2011). When the frictionless market opens in these models, any excess liquidity is absorbed so that agents start the next day being *ex ante* identical. This has been a decisive step to simplify quite substantially the rich money-search literature and develop its application in a large number of domains.

Although in this paper we focus on steady-state relations between markets, existing work has studied interesting cyclical properties of goods market frictions, and in particular in relation to the cyclical properties of intensive search margins (consumer search effort and shopping time, advertising efforts by firms). Procyclicality of goods market search effort has been established in Hall (2012) for advertising. Petrosky-Nadeau et al. (2016) provide an empirical test of the procyclicality of search effort by consumers. Their conclusions stand in contrast to Kaplan and Menzio (2013), who argue instead that consumer search effort is larger in recessions. The implications for fiscal policy in the face of procyclical disposable income, and the underlying question of fiscal multipliers, has been explored in Petrosky-Nadeau and Wasmer (2014). In Bethune et al. (2015), drops in demand from credit constrained consumers affect the labor market through a search frictional goods market in which firms' marginal revenue declines with the level of demand faced in the goods market. This mechanism also appears in Petrosky-Nadeau and Wasmer (2015).

Section 2 first introduces search in the goods market and emphasizes several important differences from classical economies, including labor search economies, that need to be clarified. The general equilibrium properties of the model are derived in the steady-state in Section 3. Price and wage bargaining solutions are explored in Section 4. We quantify the role of each friction and the various complementarities between markets in three different European economies in Section 5. Section 6 concludes.

2. A model with search in goods markets

2.1. Setup

Time is continuous. Consumers have access to two types of goods: (i) one type of good is accessible with no frictions, indexed by 0, can be thought of as a set of inferior goods (food, basic services, standard goods), and its price is normalized to unity; (ii) the other type of good, indexed by 1, is subject to search frictions, and can either be interpreted as services or the flow consumption of a durable good such as cars, housing service, etc. This second good is produced by firms, while goods 0 will be produced by consumers, as discussed below.¹

Hence, goods 0 are the goods regularly consumed without the need to search for them. Instead, goods 1 represent goods needing new search from time to time, due to both the arrival on the market of new consumption goods (e.g., a new restaurant in the neighborhood, a new brand of consumption good), or replacement of old goods previously consumed and hit by various shocks, specified below, such as changes in “consumer tastes” or the inability of firms to produce the good for a period of time.

2.2. The life cycle of a new good

A new search good can be produced through the following sequence. First, the firm develops a new project. The firm can be either an entirely new firm or an existing firm. In the latter case, this is the marginal project of that firm. This project has to be financed externally. Hence, in this early stage denoted by c , the firm attempts to form a first match with a financial intermediary. The intermediary and the “project” subsequently form a block that is called a “firm.” However, this match can break down from time to time following exogenous events, dissolving the match in the financial market. Second, this newly formed block recruits a worker in a stage denoted by v according to the standard labor matching process. Third, once the worker is recruited, the firm is able to produce and advertise to sell its good, and begins to search actively for a consumer. However, the firm does not generate profits yet. In the third phase of the life cycle of a firm, “search in the goods market” indicated by subscript g , the firm makes no revenue and incurs losses due to wage payments and operating costs. This stage precedes the final profit stage called stage π , in which it can sell to consumers and generate profits. Fig. 1 summarizes the timing and notation of the various transitions between the different stages.

In the special case of the absence of search frictions in the goods market, stages g and π are confounded. In that limiting case, stage g lasts an infinitely small amount of time. Instead, with a period of a positive length in stage g , the firm has to pay the wage to its worker, denoted by w_g . In stage π , after meeting with a consumer, the firm will obtain a price per period \mathcal{P} from the consumer who will purchase the flow of service of the goods, as a long-term relationship. This assumption characterizes the existence of specificity in the match formed in the goods market. The firm pays a wage w_π .

2.3. Random matching in labor and credit markets

As in Wasmer and Weil (2004), denote by p the rate at which the project, \mathcal{N}_c , meets the creditor, \mathcal{B}_c , and by \tilde{p} the rate at which the creditor

¹ A convenient intuition to think of the differences between the two goods is to think of the two main sources of heterogeneity across goods: spatial (similar goods are sold in different places), and horizontal (some differentiation across products). Both types of heterogeneity lead to higher search frictions. Goods 0 are goods for which search is small, because they are sold in places known to the consumers and the degree of differentiation is low enough, or because the consumer has kept a record of their location and characteristics. Goods 1 are goods for which, either locations must be found or characteristics must be investigated. Once consumed, though, they are not subject to search frictions, until the consumption match dissolves.

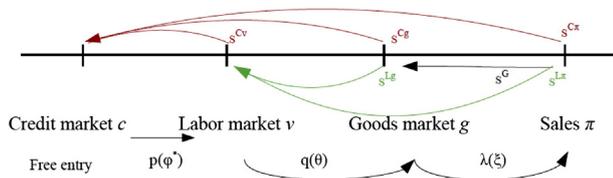


Fig. 1. Timing and transition rates of a marginal project producing the search good: credit destruction $s^{ck}, k = v, g, \pi$, labor turnover $s^{lk}, k = g, \pi$ and taste shocks τ ; credit matching rate $p(\phi)$, labor hiring rate $q(\theta)$ and goods market matching rate $\lambda(\xi)$.

meets—and implicitly both screens and accepts—the project. There is an identity in the financial market between the total number of matches, \mathcal{M}_C , the number of matched projects and the number of matched creditors in a unit of time: $\mathcal{M}_C = p\mathcal{N}_c = \check{p}\mathcal{B}_c$. The ratio of projects to creditors searching in the credit market, $\phi = \mathcal{N}_c/\mathcal{B}_c$, is a measure of conditions in the financial market called financial market tightness, and $\check{p} = \phi p$. Matching is governed by a constant returns to scale function with the mass of investment projects and creditors searching in the financial market as arguments:

$$\mathcal{M}_C(\mathcal{N}_c, \mathcal{B}_c) \quad \text{with} \quad \partial \log \mathcal{M}_C / \partial \log \mathcal{B}_c = \eta_c(\phi) \quad (1)$$

where $\eta_c(\phi)$ is the elasticity of matching in the financial market with respect to searching investment projects. The transition rates for investment projects and creditors are functions of credit market tightness with $p'(\phi) < 0$ and $\check{p}'(\phi) > 0$.

Similarly, following the macro-labor literature and [Pissarides \(2000\)](#), we assume the existence of a constant returns to scale matching function in the labor market:

$$\mathcal{M}_L = \mathcal{M}_L(\nu, \mathcal{U}) \quad \text{with} \quad \partial \log \mathcal{M}_L / \partial \log \mathcal{U} = \eta_L(\theta) \quad (2)$$

where $\theta = \nu/\mathcal{U}$ is a measure of labor market tightness and $\eta_L(\theta)$ is the elasticity of matching with respect to unemployment. We denote by $f(\theta)$ the per-unit of time rate at which unemployed workers find a job equal to $f(\theta) = \mathcal{M}_L/\mathcal{U}$, and $q(\theta) = \mathcal{M}_L/\nu$ the corresponding hiring rate from the firm's perspective. We have $f(\theta) \equiv \theta q(\theta)$ and $q'(\theta) \leq 0$.

2.4. Goods market

We denote the number of consumers matched with goods 1 or unmatched by \mathcal{D}_M and \mathcal{D}_U , respectively. We also denote by \mathcal{N}_π and \mathcal{N}_g the number of selling and searching firms (for consumers), respectively. The total number of employed workers is therefore equal to the total number of firms in each stage, that is:

$$1 - \mathcal{U} = \mathcal{N}_\pi + \mathcal{N}_g.$$

We also assume that each firm can serve only one consumer. This further implies:

$$\mathcal{D}_M \equiv \mathcal{N}_\pi.$$

This is therefore a *one-firm/one-worker/one-consumer* model.

As in the standard search and matching models, we introduce the tightness of the goods market as

$$\xi = \frac{\mathcal{D}_U}{\mathcal{N}_g}. \quad (3)$$

It follows that the transition rates for firms and for consumers are given, respectively, by

$$\frac{\mathcal{M}_G(\mathcal{D}_U, \mathcal{N}_g)}{\mathcal{N}_g} = \lambda(\xi) \quad \text{with} \quad d\lambda/d\xi > 0 \quad (4)$$

$$\frac{\mathcal{M}_G(\mathcal{D}_U, \mathcal{N}_g)}{\mathcal{D}_U} = \lambda(\xi)/\xi = \check{\lambda}(\xi) \quad \text{with} \quad d\check{\lambda}/d\xi < 0. \quad (5)$$

The total number of prospective consumers, that is, the consumers willing to exert search effort in the goods market to be able to consume search good 1, has to be determined. We assume that only employed workers, who have access to a full salary, can consume search good 1. That is, we are assuming that all income available to the unemployed is spent on essential goods; the unemployed have no additional disposable income to spend on the search good.² In this simplified economy with two goods, one (good 0) is the essential good while the other (goods 1) is a normal good or even, in the current case, a luxury good not accessible to the unemployed. It follows that the sum of unmatched and matched consumers of goods 1 sums up to total employment:

$$\mathcal{D}_U + \mathcal{D}_M = 1 - \mathcal{U}.$$

2.5. Match destruction

Labor relations in stage g and π dissolve at an exogenous Poisson rate s^{Lk} , with $k = g, \pi$. Credit relations in stage v, g , and π dissolve at an exogenous Poisson rate s^{ck} , with $k = v, g, \pi$. Although in the calibration exercise, these differences in separation rates across stages will not be very important, distinguishing them will have the virtue of following carefully the role of each parameter in the single free-entry equation condensing all the margins of the model derived in the next section. In addition, we denote by $s^{Lg, \pi}$ and $s^{cg, \pi}$ the average of these shocks across stages g and π : $s^{Lg, \pi} = (\mathcal{N}_g s^{Lg} + \mathcal{N}_\pi s^{L\pi}) / (\mathcal{N}_g + \mathcal{N}_\pi)$ and $s^{cg, \pi} = (\mathcal{N}_g s^{cg} + \mathcal{N}_\pi s^{c\pi}) / (\mathcal{N}_g + \mathcal{N}_\pi)$.

Consumer relations also dissolve, for two main reasons. First, the consumers of goods 1 may change tastes, leading to a separation of the consumer–seller relationship. Such a separation event arrives with Poisson intensity τ . Second, turnover in either the labor or credit market may terminate a worker's employment. The resulting loss of purchasing power arrives on average at rate $s^{Lg, \pi} + s^{cg, \pi}$ depending on whether the consumer is in a firm at stage g or π . This is unobserved by the selling firm. It follows that the rate of consumption-match termination s^G is the sum of the pure taste shock the consumer income shocks. We use the compact notation $s^G = \tau + s^{Lg, \pi} + s^{cg, \pi}$.

2.6. Additional notation and concepts

2.6.1. Unused production capacity

There are unused resources at the firm level. Firms have the ability to produce, but cannot necessarily sell unless they find a consumer. Production takes place only when a match with the consumer has been formed. Therefore, the firm does not use its capacity to produce in the stage where it has no consumer. The search frictions in the goods market introduce a new concept, the rate of capacity utilization. This can be defined as

$$\mu_G = \frac{\mathcal{N}_\pi}{\mathcal{N}_\pi + \mathcal{N}_g}. \quad (6)$$

The rate of capacity utilization is the ratio of firms matched with a consumer, \mathcal{N}_π , to the total number of firms matched with a worker who could, potentially, produce, $\mathcal{N}_\pi + \mathcal{N}_g = \mathcal{N}$. This rate is a widely available statistic and will be used subsequently for calibrating the frictional economy.

² The assumption that only employed workers may search for the frictional good is made for tractability, and captures the main channel of transmission from the labor to the goods market. Alternative assumptions, such as allowing the unemployed to search as well as the employed, introduce additional interactions between labor and goods markets (see [Petrosky-Nadeau and Wasmer, 2015](#)).

2.6.2. Transfers, Lucas trees, and the circular flows of income in the economy

The firm receives a unit price \mathcal{P} from consumers in exchange for x units of goods 1 produced. The good produced is assumed to be indivisible: it must be fully consumed by the consumer. Here, x must therefore be interpreted as *quality of the good*, entering the utility function of the consumer. The consumer must, in addition, have the resources at the time of the meeting with the firm to pay for the price \mathcal{P} . No credit is allowed to customers, unlike Bethune et al. (2015) and Branch et al. (2016), in which there is consumer credit.

At each point in time, there is a mass $\mu_C(1-U) = \mu_C\mathcal{N}$ of firms in stage π that is both producing and selling goods 1. In the aggregate, firms generate gross revenues $\mu_C\mathcal{N}\mathcal{P}x$, and have total wage and search costs $[\mu_C w_\pi + (1-\mu_C)w_g]\mathcal{N} + \gamma\mathcal{V}$. A fraction μ_C of firms, those in a goods market match, pay the wage w_π , while the other firms pay the wage w_g . The difference between gross revenue and costs, the net revenues generated by firms in this economy, is rebated to unemployed workers as well as employed workers in equal shares. Denote by \mathcal{K}_U and \mathcal{K}_W the dividends received by, respectively, the unemployed and employed, in the aggregate.

Importantly, workers receive additional resources, expressed in terms of the numeraire good 0, that are the fruits (in numeraire) of a Lucas tree growing in their individual garden. Each agent is endowed in each unit of time a quantity \bar{y}^0 of additional resources. Hence, total disposable income of employed workers is now:

$$(\mu_C\mathcal{P}x + \bar{y}^0)\mathcal{N} - \gamma\mathcal{V} - \mathcal{K}_U \leq \mu_C\mathcal{N}\mathcal{P}x. \tag{7}$$

In the absence of the Lucas tree ($\bar{y}^0 = 0$), and given the discussion above, consumers' aggregate net income is below the value of sales of goods 1 $\mathcal{N}\pi\mathcal{P}x$.³

2.6.3. Utility, individual and aggregate consumption

The utility function of consumers depends on the consumption of both goods 1 and 0, and of leisure denoted by l . It is denoted by $v(c^1, c^0, l)$ where the first input is consumption of the search good, the second of the numeraire, and the third leisure. We denote by c_U^0 and c_M^0 the consumption of the numeraire by, respectively, the *employed unmatched* with a search good and *employed matched* with a search good. We normalize leisure so that employed workers consume no leisure and unemployed workers may consume up to a fixed quantity of leisure denoted by z . Unmatched consumers are employed and therefore have no leisure, and a flow utility $v(0, c_U^0, 0)$. Matched consumers have a flow utility $v(x, c_M^0, 0)$.

The viability of the search economy requires that consumers prefer the frictional good to the numeraire, otherwise they would not search for good 1. The equilibrium must therefore be such that:

$$v(x, c_M^0) > v(0, c_U^0).$$

The unemployed can freely transform part or all their leisure endowment z into additional production of the numeraire, which ensures an equilibrium between demand and supply of the numeraire. Since the exact quantity of leisure transformed is irrelevant to the market equilibrium, we only report these calculations in Appendix A.

³ Under low values of \bar{y}^0 , consumers would be unable to purchase the search good. A non-degenerate equilibrium thus requires a positive and large enough value of \bar{y}^0 so that a nontrivial equilibrium exists. As evident from Eq. (7), this endowment must be greater than the sum of labor search costs and the share of dividends accruing to the unemployed, $\gamma\mathcal{V} + \mathcal{K}_U$

3. Steady-state free-entry equilibrium

3.1. Equilibrium determination strategy

Once the setup of the model has been established, we can detail the strategy of finding the steady-state equilibrium. On each of the three markets (C, L, G) the equilibrium is characterized by price $(\psi, \mathbf{w}, \mathcal{P})$ and market tightness (ϕ, θ, ξ) . Note that the wage, at this stage, is thought of as a vector since it may differ across stages of the life-cycle of the firm. The first step is to treat prices as parameters and find three equations for tightness in each market.

- Step 1. Given prices, we solve for market tightnesses (ϕ, θ, ξ) . We use the assumptions of two free-entry conditions in the credit market (for projects and creditors) to determine credit market tightness. The assumption that only the employed consume leads to determine goods market tightness ξ as the solution to the fixed-point problem independent of the equilibrium in other markets. The model is block recursive for these two tightnesses. This leaves us with a job creation equation to determine labor market tightness, which depends on wages and prices of the goods: $\theta = \Theta(\mathbf{w}, \mathcal{P})$.
- Step 2. Prices (ψ, w, \mathcal{P}) are solutions to Nash-bargaining problems. The value of repayment $\psi = \Psi(\theta)$ can be determined as a function of labor market tightness only. The good 1 price \mathcal{P} is independent of market tightness. The wage vector depends on labor market tightness: $\mathbf{w} = \mathbf{W}(\theta)$.
- Step 3. We prove existence and uniqueness of the solution to the system $\theta = \Theta(\mathbf{W}(\theta), \mathcal{P})$, and compute the equilibrium value of θ .

Once this part of the model is solved, we can calculate the remaining stocks: (i) the steady-state stock-flow equation for unemployment give U as a function of θ . Then, we obtain also $\mathcal{V} = \theta U$; (ii) the steady-state stock-flow equation for profitable firms give \mathcal{N}_g and \mathcal{N}_π (once ξ and U are known); (iii) knowing ξ and \mathcal{N}_g yields a solution for D_U , and assuming one-consumer/one-product relations gives $\mathcal{D}_M = \mathcal{N}_\pi$; (iv) the steady-state stock-flow equation for vacancies gives \mathcal{N}_c as a function of $\theta, \phi, \mathcal{N}_g$, and \mathcal{N}_π , and finally (v) we obtain \mathcal{B}_c since ϕ is known and $\phi = \mathcal{N}_c/\mathcal{B}_c$.

3.2. Bellman equations and free-entry

Upon the realization of either of the two labor market separation shocks, s^{lk} for $k = g, \pi$, the firm returns to the vacancy stage v in the entry equilibrium. Similarly, under the realization of any of the three capital market separation shocks, s^{ck} for $k = v, g, \pi$, the firm returns to the credit stage. Fig. 1 summarizes the timing of the various transitions.

Let E_c, E_v, E_g , and E_π be the respective steady-state asset values of an entrepreneur in each period (credit stage, labor stage, goods stage, and profit). Let B_c, B_v, B_g , and B_π be the respective steady-state asset values of a bank in each period (credit stage, labor stage, goods stage, and profit). The corresponding equations are in Appendix B. Under the assumption of free-entry, meaning each marginal project can enter the credit-stage freely, one has $B_c = 0$ and $E_c = 0$. Denote by J_v, J_g and J_π the firm value, that is of $E_k + B_k$ for $k = v, g, \pi$, the block formed by the "project" in different stages and the financial intermediary.

We define $K(\phi)$ as a measure of the total expected cost of financial intermediation, as the sum of expected cost of firms searching for a bank and of the expected cost of the bank searching for a suitable project to finance, that is,

$$K(\phi) = \frac{\kappa_B}{\phi p(\phi)} + \frac{\kappa_I}{p(\phi)}.$$

Under free-entry, one has:

$$(r + s^{cv})J_v = (r + s^{cv})K = -\gamma + q(\theta)(J_g - J_v) \tag{8}$$

$$(r + s^{cg})J_g = -w_g + s^{lg}(J_v - J_g) + \lambda(J_\pi - J_g) \tag{9}$$

$$(r + s^{cn})J_\pi = xP - w_\pi + s^{ln}(J_v - J_\pi) + s^g(J_g - J_\pi). \tag{10}$$

The entire model can therefore be collapsed into a single equation linking entry costs and future expected profits, by combining the recursive equations above and eliminating the value functions. We have (see Appendix B for a proof):

$$\left(1 + \frac{r + s^{cv}}{q}\right)K + \frac{\gamma}{q(\theta)} + \frac{1}{1 - Q_\pi Q_g} \left(\frac{w_g - s^{lg}K}{r + s^{lg} + s^{cg} + \lambda}\right) = \frac{Q_g}{1 - Q_\pi Q_g} \left(\frac{xP - w_\pi + s^{ln}K}{r + s^{ln} + s^{cn} + s^g}\right) \tag{11}$$

with

$$Q_g = \frac{\lambda}{r + s^{lg} + s^{cg} + \lambda}; Q_\pi = \frac{s^g}{r + s^{ln} + s^{cn} + s^g}.$$

The left-hand side is the sum of three terms, expressed in future value of the vacancy stage. The first term is the value of financial costs, the second term is the value of hiring costs, the third term is the value of wages net of the recovery costs K after labor turnover in stage g . The right-hand side is the expected discounted value of profits and recovery cost after labor turnover in stage π . It turns out that labor market tightness, if it exists, is a function of price and wages: $\theta = \Theta(w_g, w_\pi, P)$.

We will extensively study this equation and in particular calculate its various limiting components in the quantitative exercise. The expression has various limiting cases capturing the intuition of the decomposition above.

3.2.1. CL model with perfect goods market: $\lambda \rightarrow +\infty, Q_g \rightarrow 1$

In this limiting case, one obtains that the entry costs due to financial markets and the hiring costs in the labor market add up and must be equal to the present-discounted value of profits:

$$\left(1 + \frac{r + s^{cv}}{q}\right)K + \frac{\gamma}{q} = \frac{xP - w_\pi + s^{ln}K}{r + s^{ln} + s^{cn}}. \tag{12}$$

3.2.2. LG model with perfect credit markets: $K \rightarrow 0$

In this limiting case, one obtains that entry costs are the sum of hiring costs and deficits of the firm when it does not sell, and they are equal to the properly discounted sum of profits in stage π . Note that credit shocks s^c (whereby the firm is back to the entry stage $E_c = 0$) could be eliminated, but the absence of credit market imperfection does not imply the absence of such destructive shocks:

$$\frac{\gamma}{q} + \frac{1}{1 - Q_\pi Q_g} \left(\frac{w_g}{r + s^{lg} + s^{cg} + \lambda}\right) = \frac{Q_g}{1 - Q_\pi Q_g} \left(\frac{xP - w_\pi}{r + s^{ln} + s^{cn} + s^g}\right). \tag{13}$$

3.2.3. L model with both perfect credit and goods market: $K \rightarrow 0$ and $\lambda \rightarrow +\infty, Q_g \rightarrow 1$

In this limiting case, one reverts to the standard Pissarides equation where entry costs are equal to future discounted profits:

$$\frac{\gamma}{q} = \frac{xP - w_\pi}{r + s^{ln} + s^{cn}}. \tag{14}$$

3.3. Steady-state solutions for goods and credit market tightness

Going back to the general case of frictions in three markets, the model is solved recursively. The first step is to derive equilibrium goods market tightness. This is easily obtained from the steady-state equations governing the evolution of the various stocks to: (i) employment in goods market matched firms; (ii) employment in unmatched firms in the goods market; (iii) unemployment; (iv) vacancies; (v) matched consumers; and (vi) unmatched consumers. The equations for the stocks are (see Appendix C for details):

$$\mathcal{N}_\pi + \mathcal{N}_g = [1 + \lambda / (s^{lg,\pi} + s^g)]\mathcal{N}_g \tag{15}$$

$$\mathcal{D}_M + \mathcal{D}_U = [1 + \check{\lambda} / (s^{lg,\pi} + s^g)]\mathcal{D}_U \tag{16}$$

$$(\lambda + s^{lg,\pi})\mathcal{N}_g = \mathcal{N}_\pi s^g + \mathcal{M}_L(\mathcal{U}, \mathcal{V}) \tag{17}$$

$$\mathcal{M}_L(\mathcal{U}, \mathcal{V}) = s^{lg,\pi}(1 - \mathcal{U}) \tag{18}$$

$$\mathcal{N}_g + \mathcal{N}_\pi = 1 - \mathcal{U} \tag{19}$$

$$\mathcal{D}_U + \mathcal{D}_M = 1 - \mathcal{U}. \tag{20}$$

One can solve the six stock variables with the six equations above. Goods market tightness is the ratio of firms willing to sell to prospective consumers. Using the ratio of Eqs. (15) and (16) on the one hand, and along with the fact that $\mathcal{N}_g + \mathcal{N}_\pi = \mathcal{D}_U + \mathcal{D}_M$ from Eqs. (19) and (20), we have that:

$$\frac{\mathcal{N}_g + \mathcal{N}_\pi}{\mathcal{D}_M + \mathcal{D}_U} = \frac{1 + \lambda / (s^{lg,\pi} + s^g)}{1 + \check{\lambda} / (s^{lg,\pi} + s^g)} \frac{\mathcal{N}_g}{\mathcal{D}_U} = 1. \tag{21}$$

Property 1. (steady-state goods market tightness). *Consumption tightness ξ in a steady-state is equal to 1 if only the employed workers have access to the frictional good:*

$$\mathcal{D}_U + \mathcal{D}_M = \mathcal{N} \Rightarrow \xi^* = 1. \tag{22}$$

The proof amounts to solving a fixed point problem:

$$\xi = \frac{1 + \lambda(\xi) / (s^{lg,\pi} + s^g)}{1 + \check{\lambda}(\xi) / (s^{lg,\pi} + s^g)}. \tag{23}$$

Using $\check{\lambda}(\xi) = \lambda(\xi) / \xi$, it is easy to see that $\xi = 1$ is one such fixed point. It can be shown that, under an Inada condition on the matching function, there is a second fixed point $\xi = 0$ corresponding to a degenerate case with no market. This would be a subsistence economy where everyone consumes the numeraire in quantity \bar{y}^0 . There is no other fixed point for a standard matching function. When $\xi > 0$, one has $\xi + \lambda(\xi) / (s^{lg,\pi} + s^g) = 1 + \lambda(\xi) / (s^{lg,\pi} + s^g)$, which leads immediately to $\xi = 1$.⁴ This property determines not only goods market tightness, but

⁴ This result, when the ratio $(\mathcal{N}_g + \mathcal{N}_\pi) / (\mathcal{D}_M + \mathcal{D}_U)$ is equal to 1, arises from the apparently innocuous assumption that only the employed workers search for the search good. It can be interpreted as a stochastic version of the old Say's law that demand equals supply. The firm produces one good, each consumer consumes one good, and each firm employs one employee-consumer. If instead each firm employed, say, two workers, this would lead to the creation of two consumers and thus goods market tightness would be equal to 2, in the steady state. If conversely, each firm produced two units of goods, each worker-consumer would be able to consume two units of goods (in another firm) and therefore goods market tightness would be equal to half unity. Adapting this logic, if each firm could produce n_q units and employed n_w workers, the steady-state goods market tightness would be equal to n_w / n_q . Nonetheless, goods market tightness would still be a constant, a simple function of simple parameters.

also the value of transition rates in the goods market. Hence, from now on, we have $\check{\lambda}(1) = \lambda(1) = \lambda$.

In regards to the repayment ψ from the firm to the creditor in stage π , it is the solution to the following conventional Nash bargaining game:

$$\psi = \operatorname{argmax} (B_v - B_c)^{\alpha_c} (E_v - E_c)^{1 - \alpha_c}$$

where $\alpha_c \in (0,1)$ is the relative bargaining strength of the creditor. The solution to this problem depends on the assumed effect of the repayment ψ on the wage to labor w . Under the assumption that, from the perspective of bargaining in the financial market, the future wage w paid to the worker does not depend on the repayment ψ , the slopes of the value of the profit stage for both the creditor and the project are equal in absolute value. That is, $\partial B_{\pi}/\partial \psi = -\partial E_{\pi}/\partial \psi = 1/(r + s^T)$ where $s^T = s^C + s^{L\pi} + s^{C\pi}$.

It then follows that the absolute value of slopes for the asset values of the labor search stage are also equal: $\partial B_v/\partial \psi = -\partial E_v/\partial \psi = Q_L \times 1/(r + s^T)$. The Nash sharing rule for Ψ can thus be written as:

$$(1 - \alpha_c)(B_v - B_c) = \alpha_c(E_v - E_c). \tag{24}$$

The sharing rules can be rearranged as $B_v = \alpha_c J_v$ and $E_v = (1 - \alpha_c) J_v$, which states that the creditor receives a share α_c of the match surplus J_v , while a share $(1 - \alpha_c)$ accrues to the project. Recall that free entry in the financial market leads to values of the labor search stage $B_v = \kappa_B/(\phi p(\phi))$ and $E_v = \kappa_i/p(\phi)$.

Property 2. (steady-state credit market tightness). *Combining the above equations with the equation for Nash bargaining over the repayment (Eq. (24)) one reaches a unique solution for financial market tightness, ϕ^* and repayment ψ :*

$$\phi^* = \frac{\kappa_B}{\kappa_i} \frac{1 - \alpha_c}{\alpha_c} \tag{25}$$

$$\frac{\psi}{r + s^T} = \alpha_c \frac{xP - w_{\pi}}{r + s^T} + (1 - \alpha_c) \left(\frac{1 - Q_g Q_{\pi}}{Q_g} \cdot \frac{\gamma}{q(\theta)} + \frac{w_g}{\lambda} \right) \tag{26}$$

Equilibrium financial market tightness, represented in Eq. (25), is increasing in the ratio of search costs for creditor κ_B to the flow search costs for investment project κ_i . An increase in κ_B leads to fewer creditors searching in the market and hence a longer duration of search for projects. In contrast, if the creditor receives a larger share of the credit match surplus, and thus a larger share of the value of a job opening and the profit flows during production, the free entry equilibrium will have lower financial market tightness. This second property was proved in Wasmer and Weil (2004). The present discounted value of the repayment to the creditor during the profit stage, $\psi/(r + s^T)$, is an α_c weighted average of the future profit stream to the creditor-project match, $(xP - w_{\pi})/(r + s^T)$, and their past search costs in the labor and goods markets. Under perfect goods market, $\lambda \rightarrow \infty$, $Q_g = 1$, and $Q_{\pi} = 0$. In this case, the second term converges to $\gamma/q(\theta)$.

The model is now partially solved since the first two blocks, financial and goods market tightnesses, are fully determined. Price and wages now remain to be solved for, which is done next.

4. Bargaining relations in labor and goods market

Before solving for wages, one can first simplify the structure of the model. Having different turnover rates by stage of the firm led to transparent interpretations of the various parameters in the entry Eq. (11). From now on, however, we can simplify the turnover structure of the model by assuming $s^{Lg} = s^{L\pi} = s^L$ and $s^{Cv} = s^{Cg} = s^{C\pi} = s^C$, giving us:

$$rJ_v = -\gamma + q(J_g - J_v) + s^C(J_c - J_v) \tag{27}$$

$$rJ_g = -w_g + \lambda(J_{\pi} - J_g) + s^C(J_c - J_g) + s^L(J_v - J_g) \tag{28}$$

$$rJ_{\pi} = xP - w_{\pi} + s^C(J_c - J_{\pi}) + s^C(J_g - J_{\pi}) + s^L(J_v - J_{\pi}). \tag{29}$$

At each step, the existence of search frictions creates rents and those rents are conveniently split by Nash-bargaining. Nash-bargaining is commonly applied in the literature and this allows for easier comparability. We first start with a simple sequence of events where labor and goods lead to bilateral negotiations in each market, with shares of the firm/project being respectively $1 - \alpha_L$ and $1 - \alpha_C$, that is, the residual of the shares α_L and α_C of the match surpluses going to, respectively, the worker and the consumer. To simplify the exposition, we start with the case of a perfect credit market and then generalize. That is, Sections 4.1 and 4.2 present first the solution with no credit frictions ($K = 0$) called the LG model and then extend it easily to the case $K > 0$ (CLG model). Appendix B also derives the full case with $K > 0$ and different turnover rates across stages of the firm's life-cycle.

4.1. Price determination under perfect financial markets

Consumer-producer relationships are costly to create as they require several steps with direct costs (search) and have related opportunity costs. It is therefore natural to adopt a price determination rule that is the outcome of bargaining between the firm and the consumer. In what follows, on price and wage determination, we assume that bargaining takes places at the time of the meeting.

In addition, we make the simplifying assumption that workers are paid the same wage w whether or not their employer is matched with a consumer. This implies that $w_g = w_{\pi} = w$, an assumption which greatly simplifies the analysis without being central to the main results. Rigidities, in the spirit of Gertler and Trigari (2009), can justify this assumption. Alternatively, this equality of wages would arise in the presence of collective bargaining between workers and firms. Additional alternative assumptions are discussed in the concluding section, and they do not qualitatively alter the main results. Different wages and alternative timing are fully explored in Appendix F.

A newly employed worker is, by definition, a consumer not yet matched with a product in the goods market. This worker's present discounted utility is denoted by W_{n0} . After a period of random search, (s)he reaches the consumption stage 1 in which (s)he consumes the frictional good. The present discounted utility in this stage is denoted by W_{n1} . At any time, the consumer may be hit by a labor turnover shock, thus moving to unemployment and a present discounted utility of W_u . This arises with probability per unit of time s^L . Finally, a matched consumer may exit the consumption match but remain employed if a goods match termination shock occurs. These arrive at rate s^C , which includes both the taste shock τ , and the possible disruption of production due to the risk of labor turnover s^L . In both cases, the consumer returns to the goods market search stage with asset value W_{n0} .

The Bellman equations of consumers, using the earlier result that $\check{\lambda}(1) = \lambda(1) = \lambda$ in a stationary equilibrium, are:

$$rW_{n0} = v(0, \bar{y}^0 + w, 0) + \lambda(W_{n1} - W_{n0}) + s^L(W_u - W_{n0}) \tag{30}$$

$$rW_{n1} = v(x, \bar{y}^0 + w - Px, 0) + s^L(W_u - W_{n1}) + s^C(W_{n0} - W_{n1}) \tag{31}$$

$$rW_u = v(0, \bar{y}^0, z) + f(\theta)(W_{n0} - W_u) \tag{32}$$

where the last equation is based on the fact that the unemployed have an additional z units of leisure. The surplus of the consumer, $W_{n1} - W_{n0}$, is the difference in its valuation of the consumption stage and the search stage. Subtracting Eq. (30) from Eq. (31), we have the

consumer's surplus as $W_{n1} - W_{n0} = \frac{v(x\bar{y}^0 + w - \mathcal{P}x) - v(0, \bar{y}^0 + w)}{r + s^L + s^G + \lambda}$. The main results are clear under a linear utility setup. While richer dynamics require some concavity in utility v with respect to goods 0, the exposition of the main concepts of the LG model can accommodate a linear utility. Assume that $v(x, c^0) = \Phi x + c^0 + l$, where the marginal utility of goods 0 is 1 (hence it is a numeraire), and the marginal utility of goods 1 is $\Phi > 1$. A non-degenerate equilibrium will therefore require $\Phi > \mathcal{P}$. Under these preferences we obtain a simpler expression for the consumer's surplus:

$$W_{n1} - W_{n0} = \frac{\Phi x - \mathcal{P}x}{r + s^L + s^G + \lambda}.$$

The production of goods 0 has disappeared from the consumption surplus due to the assumption of linearity. The surplus from a goods market match is the present discounted value of flow net utility from consumption of the search good $(\Phi - \mathcal{P})x$. In a Walrasian market, for comparison, the price is the marginal utility of consumption of the good, and the consumer surplus is driven to zero at the equilibrium price.

In this search frictional goods market, prices are bargained and set according to a Nash-sharing rule. The price is the solution to

$$\mathcal{P} = \operatorname{argmax} (W_{n1} - W_{n0})^{\alpha_C} (J_{\pi} - J_g)^{1 - \alpha_C} \quad (33)$$

where $\alpha_C \in (0, 1)$ is the consumer's bargaining weight. The price must therefore satisfy the share rule $W_{n1} - W_{n0} = \frac{\alpha_C}{1 - \alpha_C} (J_{\pi} - J_g)$. The firm's surplus with respect to the consumer relation is, subtracting Eq. Eq. (28) from Eq. Eq. (29): $J_{\pi} - J_g = \frac{\mathcal{P}x - w_{\pi} + w_g}{r + s^L + s^G + \lambda}$.

If we make the earlier simplifying assumption that $w_g = w_{\pi}$, the wage cancels out of the surplus of the firm. Combining the definitions on the consumer and firm goods market surpluses with the Nash sharing rule leads to the bargained price:

$$\mathcal{P}x = (1 - \alpha_C)\Phi x. \quad (34)$$

The price depends on the marginal utility for the good, Φ , and the relative bargaining power of the seller $(1 - \alpha_C)$. The property that the price is a function of consumer preferences and bargaining parameters is a general one. It also arises when the wage is allowed to vary across stages g and π .

4.2. Wage determination under perfect financial markets

We make the assumption of an identical wage w at idle firms (stage g) and selling firms (stage π): $\mathbf{w} = (w_g, w_{\pi}) = (w, w)$. This wage is negotiated when the firm is in the goods market stage g . As we saw in the previous section, this assumption on wage implies that the wage does not affect the capital gain from a match in the goods market for either the consumer or the firm. The wage drops out of the expression of a match surplus for both the consumer and the firm.

The bargained wage is the outcome of

$$w = \operatorname{argmax} (J_g - J_v)^{1 - \alpha_L} (W_{n0} - W_u)^{\alpha_L}$$

leading to the labor match surplus sharing rule: $(1 - \alpha_L)(W_{n0} - W_u) = \alpha_L(J_g - J_v)$. Using the definition of the asset values, the wage can be expressed as a function of the firm's surplus with respect to the consumer:

$$w = (1 - \alpha_L)(rW_u - \bar{y}^0) + \left(\frac{\alpha_L - \alpha_C}{1 - \alpha_C}\right)\lambda(J_{\pi} - J_g)$$

and then using the expression for the seller's surplus in the previous subsection and the discounting term $Q'_g = \lambda/(r + s^L + s^G + \lambda)$, the

wage in the labor market can be linked to the price in the goods market:

$$w = (1 - \alpha_L)z + \alpha_L\gamma\theta + \left(\frac{\alpha_L - \alpha_C}{1 - \alpha_C}\right)Q'_g\mathcal{P}x. \quad (35)$$

Again, simpler cases lead to the main intuitions. The Pissarides case is obtained when $Q'_g = 1$ (frictions in the goods market disappear) and when the firm does not lose any surplus to consumers ($\alpha_C = 0$), $w = (1 - \alpha_L)z + \alpha_L(\gamma\theta + \mathcal{P}x)$.

In the general case, replacing $\mathcal{P}x$ by its equilibrium value further simplifies the wage equation to:

$$w = (1 - \alpha_L)z + \alpha_L\gamma\theta + (\alpha_L - \alpha_C)Q'_g\Phi x. \quad (36)$$

The term $(\alpha_L - \alpha_C)Q'_g\Phi x$ can more easily be understood by rewriting it as $-(1 - \alpha_L)Q'_g\Phi x + (1 - \alpha_C)Q'_g\Phi x$. The first, negative term, is a worker threat point effect: by having higher marginal utility Φx from consuming the search good, the worker has more to lose from a breakdown in negotiations as the unemployed lose access to the search good. The second one is a consumer surplus effect: the firm obtains a fraction $(1 - \alpha_C)$ of the marginal utility of the search good, and this leads to a higher wage. Simplifying, one obtains an impact of Φx that is linear in $\alpha_L - \alpha_C$. Note however that the value of $\alpha_L - \alpha_C$ is always positive: if the bargaining power of consumers were above that of workers, this would imply that the firm would give up more to the worker than what it can expect from the sales, and the total surplus would be negative in stage g . In the special case where the worker's bargaining weight in the labor market is equal to the consumer's bargaining weight in the goods market, $\alpha_L = \alpha_C$, the consumption surplus for the firm and the wage no longer depends on the price in the goods market or changes in the marginal revenue from production.

Viability conditions ensure that the decentralized equilibrium is not degenerate. The full conditions are easily derived. To summarize these conditions, it is necessary for wages to fall into the interval $(x\mathcal{P} - \bar{y}^0, x\mathcal{P})$ where \bar{y}^0 is the transfer of numeraire (income) in addition to the labor income. This means that workers can pay for the goods in numeraire and the firm can pay workers above the selling price. This condition is satisfied if the supply of numeraire \bar{y}^0 is large enough compared to a combination of parameters involving α_L and α_C as well as x, z and θ . Another condition is that unemployed workers cannot consume the inelastic supply of the search good x , which is the case when $\bar{y}^0 < x\mathcal{P} = (1 - \alpha_C)\Phi x$.

4.3. Prices and wages under imperfect credit markets

We now need to establish the setting of wages in order to determine equilibrium labor market tightness.

The prices in all three markets, the repayment to the credit ψ , the wage to the worker w , and the price for the good \mathcal{P} , are derived in the same manner as in the earlier subsections. The price equation remains a simple rule, as in the LG model, that is a function of the marginal utility of the search good Φ :

$$\text{Price : } \mathcal{P} = (1 - \alpha_C)\Phi. \quad (37)$$

Wages now incorporate the value of recoverable search costs in the financial markets, $J_v = K(\phi)$. Assuming a wage rule where the wage remains constant in stages g and π , and is negotiated in stage g to satisfy the Nash sharing rule:

$$(1 - \alpha_L)(W_{n0} - W_u) = \alpha_L(J_g - J_v)$$

one obtains a wage equation:

$$w = (1 - \alpha_L)(rW_u - \bar{y}_0) - \alpha_L(r + s^C)K + \frac{\alpha_L - \alpha_C}{1 - \alpha_C}Q'_g\mathcal{P}x \quad (38)$$

where $Q'_g = \lambda / (r + s^C + s^L + s^G + \lambda)$. Again, the wage converges to CL wage when goods market frictions disappear ($\lambda \rightarrow \infty$), to the wage in the LG model when financial frictions disappear ($K \rightarrow 0$), and to the conventional Pissarides wage when both goods and financial frictions disappear.

4.4. Viability of the market

The final step is to make sure that a positive labor market tightness is possible in equilibrium. Replacing wage and prices in the entry Eq. (11) and taking the limit when θ tends to zero, one wants the right-hand side to be larger than the left-hand side. At zero tightness, one has $rW_u = z + \bar{y}_0$; $w = (1 - \alpha_L)z - \alpha_L(r + s^C)K + (\alpha_L - \alpha_G)Q'_g x(1 - \alpha_G)\Phi$; hence $xP - w = x(1 - \alpha_G)\Phi[1 - (\alpha_L - \alpha_G)Q'_g] - (1 - \alpha_L)z + \alpha_L(r + s^C)K$ and finally the viability condition is a sufficiently high value of x relative to z :

$$K(1 - Q_\pi Q_g) + \left(\frac{(1 - \alpha_L)z - \alpha_L(r + s^C)K + (\alpha_L - \alpha_G)Q'_g x(1 - \alpha_G)\Phi - s^L K}{r + s^L + s^C + \lambda} \right) < \left(\frac{x(1 - \alpha_G)\Phi[1 - (\alpha_L - \alpha_G)Q'_g] - (1 - \alpha_L)z + \alpha_L(r + s^C)K + s^L K}{r + s^L + s^C + s^G} \right). \tag{39}$$

In a perfect goods market, when $\lambda \rightarrow \infty$, $s^G = 0$, and $\alpha_G = 0$, this viability condition states that the annuity value of credit costs must equal the production surplus:

$$(r + s^C)K < x\Phi - z.$$

Further, assuming the absence of credit frictions ($K = 0$), we obtain the familiar condition that the utility from market production should exceed the utility from leisure.

5. A quantitative exploration of the role of complementarities between the three markets

We propose in this section to calibrate the CLG model for three European economies that display strong structural differences in terms of the three markets at stake: the United Kingdom, Germany, and Spain. We use data mainly provided by Eurostat, which will be described in Section 5.1. For each country, we run a first calibration targeting 2005 data. Based on the results, some structural parameters are fixed and a second calibration is run with 2014 targets. This allows for a comparison between the three economies at two different points in time, before and after the peak of the financial crisis.

The results obtained will then be used to proceed to different numerical exercises, as described in Section 5.2. First, we can quantify the relative weight of each type of friction in the entry decision of firms in the three countries studied. The model also allows us to analyze the interdependence of the credit, labor, and goods markets. We will in particular focus on the impact of each type of friction on the unemployment rate.

5.1. Calibration strategy for three countries: Germany, UK, and Spain

The time period is monthly. In each of the frictional markets, we assume matching functions such that: $p(\phi) = \chi_C / \sqrt{\phi}$, $q(\theta) = \chi_L / \sqrt{\theta}$, and $\lambda(\xi) = \chi_G \sqrt{\xi} = \chi_G$. Table 1 summarizes the targets used for the calibration. Table 2 displays the resulting parameter values.

We first fix a set of parameters that will remain unchanged across the two time periods considered. This set includes, in the credit market, (i) the discount rate r , taken as homogenous across the three countries and matching U.S. T-bill interest rates; (ii) the creditor's bargaining power parameter α_C , assuming an equal share of surplus between

Table 1 Calibration targets: monthly frequency.

Market	Calibration target	Model	Year	UK	SPA	GER
Credit	Finance's share in GDP	Σ	2005	.024	.016	.018
			2014	.025	.013	.014
	Credit matching rate	p	2005	1/6	1/6	1/6
	Search for credit ratio	κ_B/κ_I	2005	1	1	1
Labor	Unemployment rate	u	2005	.048	.092	.110
			2014	.062	.245	.050
	Job finding rate	f	2005	.164	.167	.064
		2014	.128	.070	.103	
Wages' share in GDP		\mathcal{W}_{gdp}	2005	.578	.532	.551
			2014	.567	.515	.567
	Ratio unemployment benefits over wages	z/w	2005	.24	.46	.31
	Recruiting costs	$\gamma v/w$	2005	.036	.036	.036
Goods	Ratio of capacity utilization	μ_G	2005	.795	.803	.840
			2014	.820	.757	.840
	Numeraire's share in expenditures	η	2005	.313	.336	.344
			2014	.323	.374	.358

entrepreneur and creditor; and (iii) the credit separation rate s^C , constant over the years but varying across countries following data described in Appendix G. In addition, the level of productivity in producing the search good, x , is normalized to 1, and the quantity of numeraire in the economy \bar{y}^0 is such that agents receive one unit per year. The marginal utility of consuming the frictional good, Φ , and the pure taste shock rate, τ , are set as in Petrosky-Nadeau and Wasmer (2015).

We then proceed to calibrating a second set of parameters that are assumed to be constant over the time frame of interest (2005 to 2014) to empirical targets measured in 2005. The parameters are: (i) the credit matching parameter χ_C ; (ii) the effort cost of search for credit κ_I ; (iii) the vacancy posting cost γ , and; (iv) the level of unemployment benefits z . These four parameters are linked to four empirical moments in 2005: (i) the average length of search for credit (through the credit matching rate p); (ii) the search for credit ratio κ_B/κ_I ; (iii) the size of recruiting

Table 2 Parameter values under monthly calibration.

	Parameters	Year	UK	SPA	GER	
Fixed parameters	Discount rate	r	Both	.0033	.0033	.0033
	Credit separation rate	s^C	Both	.0028	.0034	.0011
	Bank's bargaining weight	α_C	Both	.5	.5	.5
	Productivity	x	Both	1	1	1
	Quantity of numeraire	\bar{y}^0	Both	1/12	1/12	1/12
	Marginal utility of consumption	Φ	Both	1.15	1.15	1.15
	Pure-taste shock rate	τ	Both	.01	.01	.01
Parameters calibrated to 2005 and then kept fixed for 2014	Credit matching factor	χ_C	Both	.17	.17	.17
	Credit search effort	κ_I	Both	.23	.29	.30
	Vacancy posting cost	γ	Both	.23	.55	.15
	Unemployment benefits	z	Both	.034	.056	.040
Calibrated parameters	Project screening cost	κ_B	2005	.23	.29	.30
			2014	.22	.28	.10
	Job separation rate	s^L	2005	.005	.014	.007
			2014	.006	.019	.004
	Labor matching factor	χ_L	2005	.24	.57	.12
			2014	.21	.46	.14
	Worker's bargaining weight	α_L	2005	.88	.94	.94
			2014	.90	.98	.90
	Goods matching factor	χ_G	2005	.11	.18	.14
			2014	.13	.18	.12
Consumer's bargaining power	α_G	2005	.82	.83	.84	
		2014	.83	.81	.85	

costs $\gamma\mathcal{V}/w$; and (iv) the ratio of unemployment benefits over wages z/w .

Finally, a third set of parameters are allowed to vary over time, matching the value of empirical targets measured first in 2005 and then again in 2014. These parameters are: (i) the project screening cost κ_B ; (ii) the job separation rate s^L ; (iii) the labor matching parameter χ_L ; (iv) the worker's wage bargaining power α_L ; (v) the goods matching parameter χ_G , and; (vi) the goods market bargaining parameter α_G . The empirical targets are, first, the financial sector's share in GDP $\Sigma = \frac{\psi N_n - w N_g - \gamma \mathcal{V} - \kappa_B B_c}{\bar{y}^0 + x P N_n - \gamma \mathcal{V} - \kappa_B B_c}$. Second, the unemployment rate u . Third, the job finding rate f . Fourth, the share of wages in GDP $\mathcal{W}_{gdp} = \frac{(1-u)w}{\bar{y}^0 + x P N_n - \gamma \mathcal{V} - \kappa_B B_c}$. Fifth, the rate of capacity utilization μ_G , and finally, sixth, the share of expenditure on numeraire goods in total expenditures, denoted \mathfrak{N} . We provide more details on the calibration in Appendix G, and report the values of endogenous variables in Appendix Table A.1 for completeness.

5.2. Exploring the role of frictions and their interactions

5.2.1. Decomposing the three components of entry costs

The entry Eq. (11) has three separate blocks on the left-hand side, reflecting the intensity of the entry cost due to credit, labor, and goods markets frictions:

$$\left(1 + \frac{r + s^c}{q}\right)K + \frac{\gamma}{q} + \frac{1}{1 - Q_n Q_g} \left(\frac{w_g - s^L K}{r + s^c + s^L + \lambda}\right) \tag{40}$$

$$= \frac{Q_g}{1 - Q_n Q_g} \left(\frac{x P - w_n + s^L K}{r + s^T}\right)$$

This equation also displays some interesting interaction effects between frictions in separate markets. For instance, the degree of labor market frictions amplifies the marginal effect of credit frictions summarized in K . Indeed, the lower q is, the higher will be the effect of K on total entry costs, as the cost of credit from longer periods of search in the labor market will increase. Hence, labor frictions impact both in the first term and in the second term of the entry side of the equation. Similarly, since entry wages are determined taking into account costs K , as in Eq. (38), higher financial frictions K reduce future wages. This reduces entry costs associated with goods market frictions (the third entry cost), and therefore leads to a partial substitutability between goods and financial markets.

We can compute the relative weight of each of the three blocks in the total entry costs faced by the firm as follows. In a purely accounting sense, each type of frictions is associated with an identifiable term in the sum of entry costs: $(1 + \frac{r+s^c}{q})K$ for credit, $\frac{\gamma}{q}$ for labor, and $\frac{1}{1 - Q_n Q_g} \left(\frac{w_g - s^L K}{r + s^c + s^L + \lambda}\right)$ for goods. This is illustrated in the first part of Table 3, which reports the market friction's share of total entry costs for each country to which we have calibrated the model. By construction, the sum reaches 100%.

We reach a similar conclusion when we try to isolate the contribution of each individual friction to total entry costs. To do this, the model can be solved in different particular cases where matching efficiency parameters χ_C , χ_L , or χ_G tend to infinity (i.e., the corresponding market becomes frictionless), while all other parameters are held constant. Along the way, the endogenous variables (wages, tightness, and transition rates) also change, themselves affecting the value of each component of the entry cost. For instance, having χ_C and χ_L go simultaneously to infinity leaves only the entry costs due to the initial deficit of firms trying to sell, and focuses on the role of goods market entry costs. Similarly, having χ_L and χ_G go to infinity gives the role of the entry costs due to the credit frictions. In each limiting case the value of the entry cost is compared to the total entry cost from its three components of computed prior to removing the frictions (i.e., the total cost from Eq. (40)). The results of this exercise are reported in the lower panel

Table 3

Measuring the respective role of market frictions in each market: decomposition of the three components of entry costs in 2014

Static decomposition of each block		Credit	Labor	Goods	Sum
Share of entry costs due to each friction in Eq. (40)	UK	51.6%	12.4%	36.0%	100%
	Ger	41.9%	15.8%	42.3%	100%
	Spa	80.4%	4.3%	15.3%	100%
Limit cases of an economy with only one friction	C model		L model	G model	Sum
	UK	50.8%	14.5%	48.0%	113.3%
	Ger	40.9%	18.0%	51.7%	110.7%
Size of entry costs in limiting cases relative to total initial entry costs in Eq. (40) when $\chi_j, \chi_{j'} \rightarrow +\infty$ in pairs for for $j, j' = C, L, G$, and $j \neq j'$	UK	50.8%	14.5%	48.0%	113.3%
	Spa	80.3%	5.3%	36.3%	121.9%

Note: C (resp. L, G) model refers to an economy with only credit (respectively labor, goods) frictions.

of Table 3. Note that now the sum of all columns need not be 100%, and is actually larger than 100%.

Interestingly, the share of labor market costs is small compared to the share due to the other frictions. In Spain especially, the labor block is of limited importance, while the financial block contributes over 80% of the entry cost. This may be due to the fact that, in 2014, the Spanish economy was more adversely affected by the financial crisis which severely affected banks. The fact that the goods market block is higher in the second part of the table for all countries, especially Spain, comes from the fact that labor and credit frictions reduced wages overall. Shutting them off leads to a higher entry wage, and therefore magnifies goods market frictions relative to the benchmark case.

5.2.2. Further discussion of calibration results

The results presented in Table 3 deserve some more intuition. In particular, we try to analyze why the differences in targets for the three countries lead to the obtained differences in the decomposition. Focusing on the main drivers of each component (C,L,G) of the entry equation yields valuable insights. An approximation of each term and its variations with respect to K and θ are reported in Table 4. First, the credit term $(1 + \frac{r+s^c}{q})K$ depends principally on the cost K since the parameterization is such that $r + s^c$ remains numerically small compared to q . Second, the labor term $\frac{\gamma}{q}$ is increasing in labor market tightness θ because recruiting is more difficult in a tighter market. Finally, the goods market term $\frac{1}{1 - Q_n Q_g} \left(\frac{w_g - s^L K}{r + s^c + s^L + \lambda}\right)$ is numerically equivalent to its undiscounted version w_g/λ . Goods market tightness, and therefore λ , is pinned down in the model by parameters unrelated to labor market tightness and K . The Nash bargained wage, on the other hand, depends on market conditions in both the labor and credit markets and they affect the outside options of workers and firms. As shown in Section 4.3, the wage is increasing in labor market tightness through the term W_u , the outside option for the worker, and decreasing in financial costs K , the outside option for the firm.

An approximated version of the sum of entry costs is reported in Table 4 and can be written as $\mathcal{C}(K_1) + \mathcal{L}(\theta_1) + \mathcal{G}(\theta_1, K_1)$ where the arrows in the subscripts indicate the variations of each cost with respect

Table 4

Summary of the approximation of entry costs decomposition.

Market	Original cost term	(Approximated) main component	Variations with K	Variations with θ
Credit	$(1 + \frac{r+s^c}{q})K$	$\mathcal{C}(K) = K$	↑	—
Labor	$\frac{\gamma}{q(\theta)}$	$\mathcal{L}(\theta) = \frac{\gamma}{q(\theta)}$	—	↑
Goods	$\frac{1}{1 - Q_n Q_g} \left(\frac{w_g - s^L K}{r + s^c + s^L + \lambda}\right)$	$\mathcal{G}(\theta, K) = \frac{w_g(\theta, K)}{\lambda}$	↓	↑

to the corresponding variable. The main difference between Spain and the UK or Germany concerns the labor market component. Keeping K constant, there are indeed smaller differences in credit market targets. Lower labor market tightness, as observed in Spain, has no effect on entry costs from the credit market. However, It does reduces goods and labor costs through a greater speed of matching for firms in the labor market. The share of each friction in Spain, obtained by dividing each component by the total entry cost, is a higher share of credit frictions, and a lower share for labor and goods frictions. Targets differ less between the UK and Germany. To compare the two in terms of entry costs, one can consider both higher labor market tightness and lower financial costs in Germany relative to the UK. Thus the approximation predicts a lower share of credit frictions, and a higher share of labor and goods frictions, in Germany compared to the UK, just as was found and reported in Table 3.

In sum, these examples shed light on an interesting feature of the CLG model compared to the classical search model. In the benchmark model, it is difficult to sustain a high unemployment level in equilibrium, since it implies that vacancies are filled quickly and that wages are low, making it attractive for firms to enter and thus eventually reducing unemployment. In contrast, the incorporation of other frictions in the CLG model makes it possible to reach a high unemployment rate in equilibrium, as illustrated with the case of Spain. In fact, each friction's contribution to total entry costs responds to labor market conditions, but the response of the credit market friction is negligible. As a result, high credit costs can generate high unemployment equilibria. Further, the share of credit costs in total entry costs becomes all the more important when unemployment is high (since the other two shrink). Hence, a severe labor market recession can be triggered by a financial crisis, as it was the case in Spain.

5.2.3. Demand side effects: how consumer income shocks affect entry and unemployment

Another exercise is to attempt to isolate the role of income shocks through the demand for search goods by consumers. In Eq. (40), this can be seen by observing that in total separations $s^T = s^L + s^C + s^G = 2s^L + 2s^C + \tau$, the terms s^C and s^L arise twice. This is due to the fact that the corresponding shocks, a separation in the credit market or the labor market, affect profits in two different ways. Once directly, as they capture the risk of labor turnover and credit market shocks on the expected revenue of the firm itself. Second indirectly, as these shocks affect consumers through their own firms, leading to a loss of income and the separation of the consumption relation. To decompose the two effects, it is useful to introduce a subscript, s , to the turnover shocks for the supply's direct effect on firms. We refer to this as the "classical effect." A demand side effect arises through separations indicated with the subscript d and summarized in $s^G = \tau + s_d^L + s_d^C$. We refer to this as the "consumption effect." We thus have, with this new notation:

$$s^T = s_s^L + s_s^C + s^G = s_s^L + s_s^C + \tau + s_d^L + s_d^C$$

The respective roles of these two shocks on the firm and on its consumer's income can be explored as follows. First, one can calculate the rise in labor market tightness induced by doubling labor and credit turnover shocks s_k^L, s_k^C , for both $k = s, d$, and keeping the rate of change in consumer taste constant τ . The first column in Table 4 calculates the percentage change in labor market tightness from these comparative static exercises. The effect of increasing both turnover rates simultaneously leads to a decrease of equilibrium labor market tightness. In the case of the UK, this is a 20.4% decline, 14.2% in Germany, and a larger 43.9% in Spain. The last two columns of Table 5 decompose the effect with a part due to only the supply side, thus maintaining $s^G = s_d^L + s_d^C + \tau$ fixed, and the residual part where only s^C changes. The classical effect is responsible for the largest share of the decline in labor market

Table 5

Amplification effects of supply shocks through their supplementary impact on consumer's income and demand for goods. Variation in labor market tightness when doubling the separation rates s^L and s^C individually or in combination.

	% change in θ when doubling labor and credit turnover in $\pi k = s, d$		Decomposition	
	Classical effect, supply driven $k = s$		Consumption effect, demand driven $k = d$	
UK	$s_k^L \times 2$	-11.6%	0.706	0.294
	$s_k^C \times 2$	-9.8%	0.821	0.179
	$s_k^L, s_k^C \times 2$	-20.4%	0.772	0.228
Germany	$s_k^L \times 2$	-10.2%	0.719	0.281
	$s_k^C \times 2$	-4.5%	0.825	0.175
	$s_k^L, s_k^C \times 2$	-14.2%	0.758	0.242
Spain	$s_k^L \times 2$	-36.1%	0.806	0.194
	$s_k^C \times 2$	-11.3%	0.853	0.147
	$s_k^L, s_k^C \times 2$	-43.9%	0.830	0.170

Classical effect: contribution of supply-driven separations, keeping demand-driven separations $s^G = s_d^L + s_d^C + \tau$ fixed. Consumption effect: contribution of demand-driven separations, keeping supply-driven separations s_s^L, s_s^C fixed.

tightness, ranging between 70% and 85% depending on the country. Nonetheless, the demand effect is a non-negligible component of the effect of turnover on labor market tightness. These results provide an upper bound on the depressing effect of the lack of consumption sharing in this economy.

5.2.4. The respective role of each friction on unemployment

The model in steady-state offers comparative statics exercises for the respective role of different frictions. Investigating the impact of each friction separately or simultaneously is likely to deliver different outcomes because of potential interactions among the frictions. As said above, there is both complementarity and substitutability across frictions.

To better understand the pattern of complementarity, we represent in Fig. 2 the left-hand side (costs) and the right-hand side (profits) of the entry equation, as a function of labor market tightness, and double the efficiency of the three markets one by one. The solid lines are the entry and profit curves in the benchmark economy. The dashed lines represent the same curve after a doubling of the efficiency of each market separately: respectively, credit, labor, and goods market when going from left to right.

It can be seen that the greatest impact on curves is the effect of a change in the efficiency of credit market matching. This shifts entry down, as expected, since a 1% increase in χ_C reduces K by the same amount, and these costs represent more than 50% of total entry costs. However, the total effect on labor market tightness is not large. This is because the higher efficiency of matching in the credit market is partly offset by lower future profits, due to higher wages and a lower "recovery value" after labor separation. In contrast, changes in the efficiency of labor markets reduces entry costs as well. This leads to larger increases in labor market tightness, with no impact on the profit curve. Finally, an increase in the efficiency of goods market matching has both a downward effect on costs and an ambiguous effect on profits as part of the effect appears in wages. However, the latter effect is small and, overall, the main effect is to increase labor market tightness as well.

Table 6 shows the effects of varying matching efficiency in each market on labor market tightness. The slope of this effect varies across countries, but a 10% increase in matching efficiency in credit market raises tightness by 8.6% in the UK, 7% in Germany, and 7.6% in Spain (implying elasticities of, respectively, 0.86, 0.7, and 0.76). Note that this effect declines with the size of the efficiency increase. Similarly, a 10% increase in matching efficiency in labor market raises tightness by 9.3% in the UK, 8.5% in Germany, and a larger 30.5% in Spain (implying elasticities of,

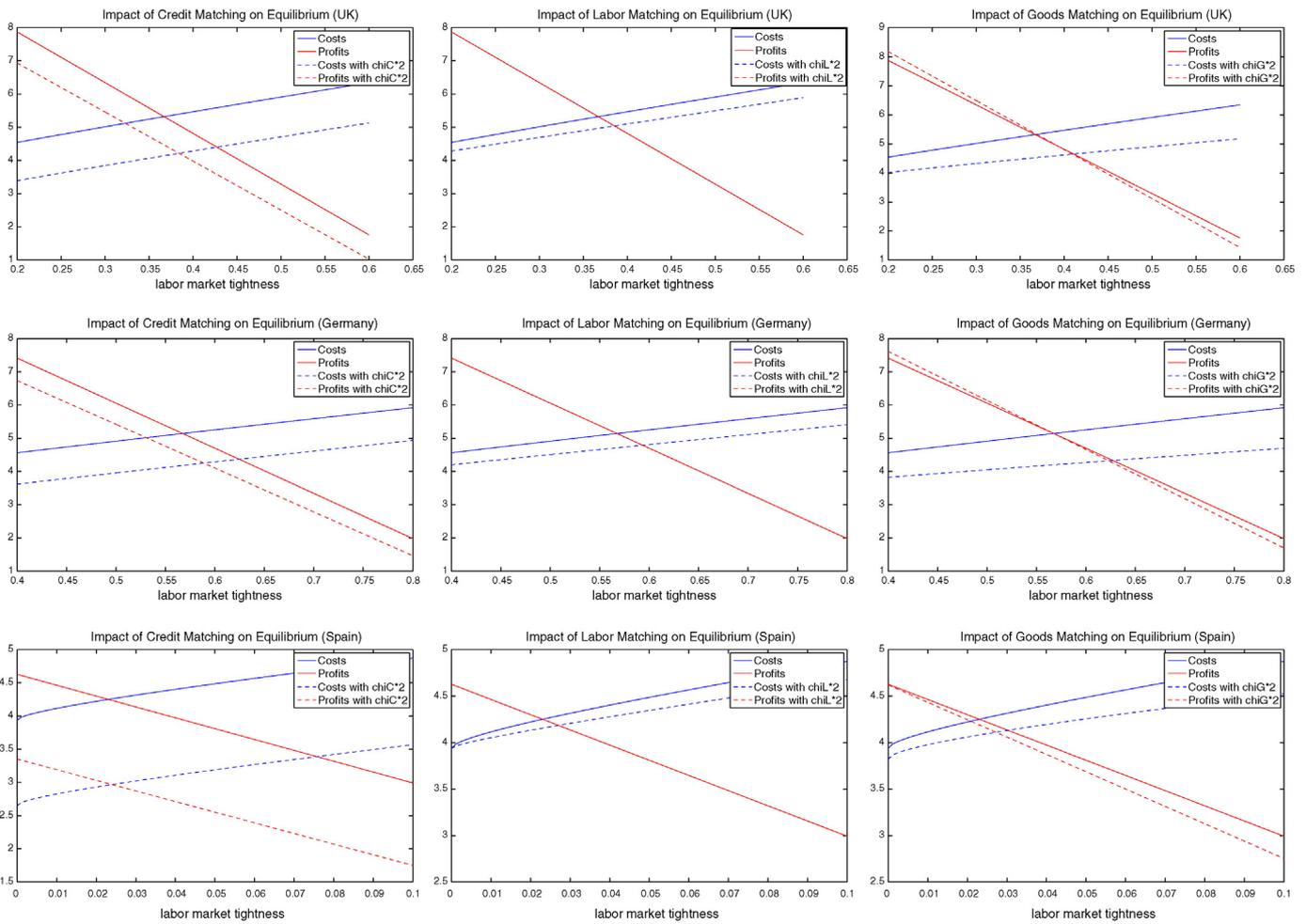


Fig. 2. Effect of doubling each matching efficiency parameter $\chi_j, j = C,L,G$ on the entry costs curve and the profit curve as a function of labor market tightness. Left charts: doubling credit matching efficiency; middle charts: doubling labor matching efficiency; right charts: doubling goods matching efficiency.

respectively, 0.93, 0.85, and 3.05). Finally, an increase in goods market efficiency generates an increase in labor market tightness of 20.1%, 17.3%, and 30.5% (implying elasticities of, respectively, 2.01, 1.73, and 3.05). Larger elasticities correspond to the case of smaller total surplus (especially for Spain) and the friction considered having a greater impact on that surplus; with small surpluses, the economy is more volatile to shocks. Note also that cross-market effects tend to attenuate each other: lower frictions in one market reduce the marginal impact of reducing frictions in another market. This effect comes from the wage effect of frictions. Higher efficiency of matching raises wages through

both lower K and higher θ , and the second-order derivatives of θ with respect to two frictions are negative. In the case of fixed wages, one would have instead $\frac{\Delta^2 \theta}{\Delta \chi_C \Delta \chi_L} = \frac{\Delta^2 \theta}{\Delta \chi_C \Delta \chi_L} = 0$, while elasticities of labor market tightness to efficiency of matching is typically 10 times higher, an effect well known in the literature following Shimer (2005) and Hall (2005).

Finally, and as expected from Fig. 2, the main effect on unemployment reported in Table 7 comes from reducing labor market frictions, despite the potentially larger impact of credit market frictions: reducing credit market frictions pushes entry cost down on the credit side, but

Table 6
Percentage (log-variation) in θ from changes in matching efficiency.

% $\Delta \chi_j, j = C,L,G$	UK				Germany				Spain			
	+10	+33	+50	+100	+10	+33	+50	+100	+10	+33	+50	+100
<i>One parameter increases</i>												
$\frac{\Delta \theta}{\Delta \chi_C}$	8.6	7.9	7.5	6.6	7.0	6.4	6.0	5.3	7.6	6.9	6.6	5.8
$\frac{\Delta \theta}{\Delta \chi_L}$	9.3	8.4	8.0	7.0	8.5	7.7	7.3	6.4	30.5	27.8	26.3	23.1
$\frac{\Delta \theta}{\Delta \chi_G}$	20.1	18.6	17.7	15.7	17.3	15.9	15.2	13.5	30.5	28.3	27.0	24.1
<i>Two parameters increase: complementarities</i>												
$\frac{\Delta^2 \theta}{\Delta \chi_C \Delta \chi_L}$	-4.6	-4.0	-3.8	-3.3	-4.7	-3.6	-3.5	-3.1	-12.9	-11.9	-11.4	-10.1
$\frac{\Delta^2 \theta}{\Delta \chi_C \Delta \chi_G}$	-4.6	-4.1	-3.9	-3.4	-3.4	-2.5	-2.3	-2.0	-12.8	-11.7	-11.0	-9.7
$\frac{\Delta^2 \theta}{\Delta \chi_L \Delta \chi_G}$	-9.5	-8.8	-8.4	-7.5	-8.2	-7.6	-7.3	-6.5	-12.9	-12.0	-11.5	-10.3

Table 7
Unemployment rate effect of increase in matching efficiency.

Baseline rate [$-0.075\ln$] % $\Delta\chi_j$	UK: 6.2				Germany: 5.0				Spain: 24.5			
	+10	+33	+50	+100	+10	+33	+50	+100	+10	+33	+50	+100
$j = C,L,G$												
χ_C	6.2	6.1	6.1	6.0	4.9	4.9	4.9	4.9	24.4	24.3	24.2	24.1
χ_L	5.6	4.7	4.1	3.1	4.5	3.7	3.3	2.5	22.5	19.0	17.0	13.0
χ_G	6.1	6.0	6.0	5.9	4.9	4.9	4.8	4.7	24.2	23.7	23.5	22.9
χ_C, χ_L	5.6	4.6	4.1	3.0	4.5	3.7	3.3	2.4	22.4	18.8	16.8	12.8
χ_L, χ_G	5.6	4.5	4.0	3.0	4.5	3.7	3.2	2.4	22.2	18.4	16.3	12.1
χ_C, χ_G	6.1	6.0	5.9	5.7	4.9	4.8	4.8	4.7	24.1	23.5	23.2	22.6
χ_C, χ_L, χ_G	5.6	4.5	3.9	2.9	4.5	3.6	3.2	2.3	22.2	18.2	16.1	12.0

Table 8
Robustness of the decomposition in terms of the share of entry costs.

Friction	UK				Germany				Spain			
	C	L	G	Sum	C	L	G	Sum	C	L	G	Sum
Benchmark	51.6	12.4	36.0	100	41.9	15.8	42.3	100	80.4	4.3	15.3	100
<i>Finance's share in GDP</i>												
$\Sigma \times 2$	45.9	13.2	40.9	100	34.4	17.4	48.2	100	78.1	4.8	17.2	100
$\Sigma/10$	56.6	11.5	31.9	100	47.5	14.5	38.0	100	82.7	3.8	13.5	100
<i>Credit-search costs</i>												
$\kappa_B = 2\kappa_j$	51.6	12.4	36.0	100	41.9	15.8	42.3	100	80.4	4.3	15.3	100
$\kappa_B = \kappa_j/2$	51.6	12.4	36.0	100	41.8	15.8	42.4	100	80.4	4.3	15.3	100
<i>Credit finding rate</i>												
$p \times 2$	51.6	12.4	36.0	100	41.9	15.8	42.3	100	80.4	4.3	15.3	100
$p/2$	51.6	12.4	36.0	100	41.8	15.8	42.4	100	80.4	4.3	15.3	100
<i>Creditor's bargaining power</i>												
$\alpha_C = 0.8$	51.3	12.4	36.3	100	41.1	15.6	43.3	100	80.9	4.2	15.0	100
$\alpha_C = 0.2$	50.5	12.5	37.0	100	41.5	16.2	42.3	100	78.9	4.7	16.4	100
<i>Quantity of numeraire</i>												
$\bar{y}^0 \times 2$	51.7	12.4	35.8	100	42.3	15.8	41.9	100	80.4	4.3	15.2	100
$\bar{y}^0 / 2$	50.7	12.5	36.8	100	35.9	16.9	47.2	100	80.3	4.4	15.4	100
<i>Marginal utility of search good</i>												
$\Phi = 1.2$	51.6	12.4	36.0	100	41.9	15.8	42.3	100	80.4	4.3	15.3	100
$\Phi = 1.1$	51.6	12.4	36.0	100	41.9	15.8	42.3	100	80.4	4.3	15.3	100

the rise in wages mitigates this effect and ex-post turns out to almost eliminate the gains. In particular, in the UK, doubling the efficiency of goods and credit markets would reduce the rate of unemployment by 3.1 percentage points. In Germany, the effect would be 2.5 percentage points. In Spain, the effect would be 11.5 percentage points.

5.3. Robustness to variations in targets or in fixed parameters

The robustness of our results is tested by varying the parameters for which we either have no target in the data or uncertain targets.

From top to bottom, Table 8 shows the decomposition of the three entry costs to: a doubling or a division by 10 of the share of finance (business sector) in GDP⁵; a doubling or a division by 2 of the relative costs of credit search of creditors relative to projects/firms; a doubling or a division by 2 of the transition rate of projects/firms from search for credit to the labor stage; a change of the bargaining power of creditors vis-à-vis the firm to 0.9 or 0.2; a doubling or a division by 2 of the

⁵ We had attributed half of the total finance share to the business sector, the other half being, in national accounts, services to consumers. This is close to the division for U.S. data but not necessarily applicable to the countries studied here. Note that reducing the value added of the financial sector relative to GDP raises the prospecting costs in the calibration when α_C is fixed. Doing so reduces the profit margins of the financial sector, which in turn raises the share of credit in total entry costs.

exogenous injections of Lucas fruits into the economy, and finally, a change in the marginal utility of search goods by 10% or 20%. As is apparent, changes in the decomposition are rarely important compared to the benchmark case. In some cases, they are even totally neutralized in the entry equation by proportional comovements of the three components, as is the case for changes in the marginal utility of search goods or varying the duration of credit search $1/p$. The same conclusion is reached when replicating the decomposition exercise reported in the lower part of Table 3. See Table A.2 in the Appendix for the detailed results.

6. Conclusion

This paper has proposed a simplified structure for complex economies with imperfect credit, labor, and goods markets. We have shown how to solve them in the steady-state with a rich structure of bargaining over prices, wages, and financial repayments, and in the presence of turnover rates specific to each phase of the firm, thus generalizing our previous approach (Petrosky-Nadeau and Wasmer (2015)). We then apply this model by calibrating it to three European economies.

We find that, for these countries, goods and credit market frictions are a dominant share of entry costs leading to the creation of jobs. As a result, we conclude that they deserve much more attention in the

quantitative macroeconomic literature. Along similar lines, [Pissarides \(2009\)](#) showed how noncyclical entry costs considerably improve the fit of the search and matching model to U.S. data. Our work provides a micro-foundatio for such costs built on search friction credit and goods markets. We also find that demand side effects, through individual income shocks that affect the demand for goods, are an element of the data but are not extremely important. They account for, at most, 15% to 25% of the effect of job destruction shocks on aggregate labor market tightness. Lastly, we find that the respective speeds of matching in the goods market and the credit market both have small effects on labor market tightness, and this represents weak margins to improve outcomes such as the level of unemployment. Increasing the speed of matching in the labor market is the most effective. The general conclusion is that the richer models of the CLG type considerably improve our quantitative understanding of the labor market equilibrium.

Appendix A. Demand and supply of numeraire

The unemployed can transform part or all their leisure endowment z into additional production of the numeraire. This fixes the demand and supply of the numeraire. Denote by dz this fraction transformed into numeraire, where d might be smaller or larger than 1 (in the latter case the unemployed would enjoy negative leisure, that is exert more effort than the employed workers). They therefore supply $zd + \bar{y}^0$ units of good 0, and receive in turn a flow utility $v(0, \bar{y}^0 + zd, z(1-d))$. Under the additional assumption that leisure and consumption of good 0 are additively separable in the utility function, the value of d is irrelevant hereafter in the utility of the unemployed. However, as shown below, this value matters to equalize the demand and supply of the numeraire.

Since it is assumed there is no saving or pooling of income across individuals, a consumer not matched with a search good spends his disposable income denoted by w on the numeraire. Thus, $c_U^0 = w + \bar{y}^0$. Matched consumers must sacrifice some consumption of the essential good in order to buy the search good. Thus, the consumption of good 0 of a matched consumer is $c_M^0 = c_U^0 - pX = \bar{y}^0 + w - pX$.

We denote by $C^1 = xD_M$ the aggregate consumption of search goods 1. The aggregate consumption of good 0 is given by

$$C^0 = (U + D_U)\bar{y}^0 + D_U w + D_M(\bar{y}^0 + w - pX).$$

It is the sum of individual consumption of the unemployed, of the unmatched consumers, and of the matched consumers. The above equation implies that the supply of numeraire $zdU + \bar{y}^0$ equals its demand. Using $U + D_U + D_M = 1$, the equality implies $D_U w + D_M(w - pX) = zdU$ or equivalently

$$Nw - D_M pX = zdU.$$

This equation states that the revenue from firms net of expenses into the search good are spent in the supplementary numeraire provided by the transformation of leisure of the unemployed. Therefore, d adjusts here to equalize demand and supply of the numeraire. It is important to note that, once the fraction d of leisure transformed into numeraire to equalize demand and supply is determined, its value disappears from the rest of the model. Only z will affect the equilibrium wages and therefore labor market tightness.

Appendix B. The general entry equation

We have the fundamental Bellman equations:

$$rE_c = -\kappa_l + p(\phi)(E_v - E_c) \tag{41}$$

$$rE_v = -\gamma + \gamma + q(E_g - E_v) + s^{cv}(E_c - E_v) \tag{42}$$

$$rE_g = -w_g + w_g + \lambda(E_\pi - E_g) + s^{cg}(E_c - E_g) + s^{lg}(E_v - E_g) \tag{43}$$

$$rE_\pi = xP - w_\pi - \psi + s^{cn}(E_c - E_\pi) + s^G(E_g - E_\pi) + s^{ln}(E_v - E_\pi) \tag{44}$$

and

$$rB_c = -\kappa_b + \phi p(\phi)(B_v - B_c) \tag{45}$$

$$rB_v = -\gamma + q(B_g - B_v) + s^{cv}(B_c - B_v) \tag{46}$$

$$rB_g = -w_g + \lambda(B_\pi - B_g) + s^{cg}(B_c - B_g) + s^{lg}(B_v - B_g) \tag{47}$$

$$rB_\pi = \psi + s^{cn}(B_c - B_\pi) + s^G(B_g - B_\pi) + s^{ln}(B_v - B_\pi) \tag{48}$$

Summing up two-by-two, one obtains the value in the text:

$$(r + s^{cv})J_v = -\gamma + q(\theta)(J_g - J_v) \tag{49}$$

$$(r + s^{cg})J_g = -w_g + s^{lg}(J_v - J_g) + \lambda(J_\pi - J_g) \tag{50}$$

$$(r + s^{cn})J_\pi = xP - w_\pi + s^{ln}(J_v - J_\pi) + s^G(J_g - J_\pi) \tag{51}$$

Two convenient notations can be introduced: let

$$Q_g = \frac{\lambda}{r + s^{lg} + s^{cg} + \lambda} \quad ; \quad Q_\pi = \frac{s^G}{r + s^{ln} + s^{cn} + s^G}$$

which allows to rewrite Eqs. (50) and (51) as

$$J_g = \left(\frac{s^{lg}K - w_g}{\lambda} + J_\pi \right) Q_g \tag{52}$$

$$J_\pi = \left(\frac{xP - w_\pi + s^{ln}K}{s^G} + J_g \right) Q_\pi. \tag{53}$$

Solutions follow: one has then

$$J_g = \left[\frac{s^{lg}K - w_g}{\lambda} + \left(\frac{xP - w_\pi + s^{ln}K}{s^G} + J_g \right) Q_\pi \right] Q_g \tag{54}$$

$$J_\pi = \left[\frac{xP - w_\pi + s^{ln}K}{s^G} + \left(\frac{s^{lg}K - w_g}{\lambda} + J_\pi \right) Q_g \right] Q_\pi \tag{55}$$

or after simplification:

$$J_g = \frac{Q_g}{1 - Q_\pi Q_g} \left[\frac{s^{lg}K - w_g}{\lambda} + \left(\frac{xP - w_\pi + s^{ln}K}{s^G} \right) Q_\pi \right] \tag{56}$$

$$J_\pi = \frac{Q_\pi}{1 - Q_\pi Q_g} \left[\frac{xP - w_\pi + s^{ln}K}{s^G} + \left(\frac{s^{lg}K - w_g}{\lambda} \right) Q_g \right]. \tag{57}$$

Eq. (49) combined with free-entry $J_v = K$ immediately delivers:

$$\left(1 + \frac{r + s^{cv}}{q} \right) K + \frac{\gamma}{q} = J_g \tag{58}$$

$$\left(1 + \frac{r + s^{cv}}{q} \right) K + \frac{\gamma}{q} = \frac{Q_g}{1 - Q_\pi Q_g} \left[\frac{s^{lg}K - w_g}{\lambda} + \left(\frac{xP - w_\pi + s^{ln}K}{s^G} \right) Q_\pi \right]. \tag{59}$$

Eq. (59) can be rewritten by putting entry costs including early wages w_g on the left-hand side and rearranging it, so as to have:

$$\left(1 + \frac{r + s^{cv}}{q}\right)K + \frac{\gamma}{q} + \frac{Q_g}{1 - Q_\pi Q_g} \left(\frac{w_g - s^{lg}K}{\lambda}\right) = \frac{Q_g Q_\pi}{1 - Q_\pi Q_g} \left(\frac{xP - w_\pi + s^{L\pi}K}{s^G}\right) \quad (60)$$

$$\text{or } \left(1 + \frac{r + s^{cv}}{q}\right)K + \frac{\gamma}{q} + \frac{1}{1 - Q_\pi Q_g} \left(\frac{w_g - s^{lg}K}{r + s^{lg} + s^{cg} + \lambda}\right) = \frac{Q_g}{1 - Q_\pi Q_g} \left(\frac{xP - w_\pi + s^{L\pi}K}{r + s^{L\pi} + s^{c\pi} + s^G}\right) \quad (61)$$

$$\text{or finally } K + Q_v \frac{\gamma}{q} + \frac{Q_v Q_g}{1 - Q_\pi Q_g} \left(\frac{w_g - s^{lg}K}{\lambda}\right) = \frac{Q_v Q_g Q_\pi}{1 - Q_\pi Q_g} \left(\frac{xP - w_\pi + s^{L\pi}K}{s^G}\right) \quad (62)$$

with (63)

$$Q_g = \frac{\lambda}{r + s^{lg} + s^{cg} + \lambda}; Q_\pi = \frac{s^G}{r + s^{L\pi} + s^{c\pi} + s^G}; Q_v = \frac{q}{r + s^{cv} + q}. \quad (64)$$

Appendix C. Stock-flow equations in the extensive margin CLG model

In this part, we assume from the start the existence of credit shocks leading to the destruction of the firm in stages g and π . The stock of firms in stage π receives the matches created in the goods market λN_g and loses the firms in stage π , losing their workers $s^{L\pi} N_\pi$, the consumers quitting the good $s^G N_\pi$ and finally the firms destroyed by credit shocks $s^C D_M$. The stock of firms in stage g receives the hirings M_L and the firms losing their clients $s^G N_\pi$, and loses the matches created in the goods market λN_g and loses the firms in stage g losing their workers $s^{Lg} N_g$ as well as those hit by a credit shock $s^{Cg} N_g$.

The stock of matched consumers receives the matches created in the goods market λD_U , loses the matched consumers who lost their job $s^{Lg,\pi} D_M$ which occurs either with probability s^{Lg} or $s^{L\pi}$ depending on whether the consumer is himself/herself in a firm in stage g or π selling (hence the compact notation $s^{Lg,\pi} = s^{Lg} N_g + s^{L\pi} N_\pi / (N_g + N_\pi)$ for the expected turnover rate in stage g) and loses the consumers whose firm lost their worker $s^L D_M = (s^G - \tau) D_M$; and loses the consumers who changed taste τD_M . The stock of unmatched consumers loses the matches created in the goods market λD_U , gains the matches created in the labor market M_L , gains the consumers whose firm lost their worker $s^L D_M$ and loses the unmatched consumers who lost their job $s^{Lg,\pi} D_U$ and gains the consumers who changed taste τD_M . Finally, the pool of unemployed workers loses the matches creates in the labor market M_L , gains the job losses $s^{Lg,\pi} (1 - U)$ which arise, from the firm side, from firms in stage π losing their workers $s^{L\pi} N_\pi$ and firms in stage g losing their workers $s^{Lg} N_g$; or from matched consumers losing their job $s^L D_M$ or from unmatched consumers losing their job $s^L D_U$:

$$\frac{\partial N_\pi}{\partial t} = \underbrace{\lambda N_g}_{\text{matches G}} - \underbrace{s^{L\pi} N_\pi}_{\text{loss workers}} - \underbrace{s^G N_\pi}_{\text{loss customer}} - \underbrace{s^C N_\pi}_{\text{credit shock}} \quad (65)$$

$$\frac{\partial N_g}{\partial t} = \underbrace{M_L(U, V)}_{\text{matches L}} + \underbrace{s^G N_\pi}_{\text{loss customer}} - \underbrace{\lambda N_g}_{\text{matches G}} - \underbrace{s^{Lg} N_g}_{\text{loss workers}} - \underbrace{s^{Cg} N_g}_{\text{credit shock}} \quad (66)$$

$$\frac{\partial D_M}{\partial t} = \underbrace{\lambda D_U}_{\text{matches G}} - \underbrace{s^{L\pi} D_M}_{\text{seller loses worker}} - \underbrace{s^{C\pi} D_M}_{\text{seller hit by a credit shock}} - \underbrace{s^{Lg,\pi} D_M}_{\text{matched consumer loses job}} - \underbrace{\tau D_M}_{\text{matched consumer changes tastes}} \quad (67)$$

$$\frac{\partial D_U}{\partial t} = \underbrace{-\lambda D_U}_{\text{matches G}} + \underbrace{\tau D_M}_{\text{matched consumer changed tastes}} + \underbrace{M_L(U, V)}_{\text{matches L}} + \underbrace{s^{L\pi} D_M}_{\text{seller loses worker}} + \underbrace{s^{C\pi} D_M}_{\text{seller hit by a credit shock}} - \underbrace{s^{Lg,\pi} D_U}_{\text{unmatched consumer loses job}} \quad (68)$$

$$\frac{\partial U}{\partial t} = -M_L(U, V) + (s^{Lg,\pi} + s^{Cg,\pi})(1 - U) = -M_L(U, V) + (s^{L\pi} + s^{C\pi})(N_\pi + N_g) - M_L(U, V) + (s^{Lg,\pi} + s^{Cg,\pi})(D_U + D_M) \quad (69)$$

One can easily verify that $\partial N_\pi / \partial t + \partial N_g / \partial t + \partial U / \partial t = 0$ and that $\partial D_M / \partial t + \partial D_U / \partial t + \partial U / \partial t = 0$ at the same time.

Appendix D. Price determination in CLG

Start from

$$(r + s^{c\pi})J_\pi = xP - w_\pi + s^{L\pi}(J_v - J_\pi) + s^G(J_g - J_\pi) \\ rW_{n1} = (\Phi - P)x + \bar{y}_0 + s^G(W_{n0} - W_{n1}) + (s^{L\pi} + s^{c\pi})(W_u - W_{n1})$$

and

$$rW_{n0} = \bar{y}_0 + W_g + \lambda(W_{n1} - W_{n0}) + (s^{L\pi} + s^{c\pi})(W_u - W_{n0}) \\ (r + s^{cg} + s^{lg})J_g = -w_g + s^{lg}K + \lambda(J_\pi - J_g).$$

Note that we needed here $s^{L\pi} = s^{lg}$ otherwise two types of consumers. This leads to the firm's and consumer's consumption surpluses:

$$(r + s^{c\pi} + s^{L\pi} + s^G)(J_\pi - J_g) = xP - w_\pi + s^{L\pi}K - J_g(r + s^{c\pi} + s^{L\pi}) \\ = xP - w_\pi + s^{L\pi}K - (-w_g + s^{lg}K + \lambda(J_\pi - J_g)) \\ (r + s^{c\pi} + s^{L\pi} + s^G)(W_{n1} - W_{n0}) \\ = (\Phi - P)x + \bar{y}_0 + (s^{L\pi} + s^{c\pi})(W_u - W_{n0}) - rW_{n0} \\ = (\Phi - P)x + \bar{y}_0 + (s^{L\pi} + s^{c\pi})(W_u - W_{n0}) - (\bar{y}_0 + \lambda(W_{n1} - W_{n0}) \\ + (s^{L\pi} + s^{c\pi})(W_u - W_{n0})) \\ = (\Phi - P)x - \lambda(W_{n1} - W_{n0}).$$

Bargaining over prices thus leads to, through $(W_{n1} - W_{n0})(1 - \alpha_C) = (J_\pi - J_g)\alpha_C$:

$$\alpha_C [xP - w_\pi + s^{L\pi}K - (-w_g + s^{lg}K + \lambda(J_\pi - J_g))] \\ = (1 - \alpha_C)[(\Phi - P)x - \lambda(W_{n1} - W_{n0})]$$

and finally leads to:

$$P x = (1 - \alpha_C)\Phi x + \alpha_C [w_\pi - w_g - s^{L\pi}K + s^{lg}K].$$

In the special case where wages are identical (see below), the price converges to a constant of parameters,

$$P_X = (1 - \alpha_G)\Phi_X + \alpha_G(s^{Lg} - s^{L\pi})K$$

which is even further simplified when labor turnover is the same in both stages g and π .

$$P_X = (1 - \alpha_G)\Phi_X.$$

Appendix E. Wage determination in stage g of CLG

Assume that the wage remains constant between stages g and π and utility is linear. The labor surpluses of workers and bargaining firms are stages g and π and utility is linear. The labor surpluses of workers and bargaining firms are

$$\begin{aligned} (r + s^{Lg} + s^{Cg})(W_{n0} - W_u) &= \bar{y}_0 + w_g + \lambda(W_{n1} - W_{n0}) - rW_u \\ (r + s^{Cg} + s^{Lg})(J_g - J_v) &= 0 - w_g + \lambda(J_\pi - J_g) - (r + s^{Cg})K \end{aligned}$$

with

$$rW_u = \bar{y}_0 + f(W_{n0} - W_u).$$

The capital gain of the worker when (s)he accesses consumption good 1 $W_{n1} - W_{n0}$ is independent of w_g . The same is true from the capital gain of the firm $J_\pi - J_g$. The maximization of the Nash product in the labor market therefore leads to: $(1 - \alpha_L)(W_{n0} - W_u) = \alpha_L(J_g - J_v)$ leading to:

$$\begin{aligned} (1 - \alpha_L)[\bar{y}_0 + w_g + \lambda(W_{n1} - W_{n0}) - rW_u] \\ = \alpha_L[-w_g + \lambda(J_\pi - J_g) - (r + s^{Cg})K] \\ \Leftrightarrow w_g = \alpha_L[0 - (r + s^{Cg})K] + (1 - \alpha_L)(rW_u - \bar{y}_0) \\ + \lambda\alpha_L(J_\pi - J_g) - (1 - \alpha_L)\lambda(W_{n1} - W_{n0}). \end{aligned}$$

Interestingly, the latter term can be simplified using the price bargaining equation, which holds in expectation and in equilibrium, delivering the wage equation:

$$w_g = (1 - \alpha_L)(rW_u - \bar{y}_0) + \alpha_L[-(r + s^{Cg})K] + \lambda(J_\pi - J_g) \frac{\alpha_L - \alpha_G}{1 - \alpha_G}$$

One can also replace the surplus of the firm by its forward value, using again

$$J_g = \frac{Q_g}{1 - Q_\pi Q_g} \left[\left(\frac{s^{Lg}K - w_g}{\lambda} \right) + \left(\frac{xP - w_\pi + s^{L\pi}K}{s^G} \right) Q_\pi \right] \tag{70}$$

$$J_\pi = \frac{Q_\pi}{1 - Q_\pi Q_g} \left[\left(\frac{xP - w_\pi + s^{L\pi}K}{s^G} \right) + \left(\frac{s^{Lg}K - w_g}{\lambda} \right) Q_g \right] \tag{71}$$

one has:

$$\begin{aligned} J_\pi - J_g &= \frac{1}{1 - Q_\pi Q_g} \left[Q_\pi \left(\frac{xP - w_\pi + s^{L\pi}K}{s^G} \right) + \left(\frac{s^{Lg}K - w_g}{\lambda} \right) Q_g Q_\pi - Q_g \frac{s^{Lg}K - w_g}{\lambda} \right. \\ &\quad \left. - \left(\frac{xP - w_\pi + s^{L\pi}K}{s^G} \right) Q_\pi Q_g \right] \\ &= \frac{1}{1 - Q_\pi Q_g} \left[[1 - Q_g] \left(\frac{xP - w_\pi + s^{L\pi}K}{s^G} \right) + \left(\frac{s^{Lg}K - w_g}{\lambda} \right) [Q_g Q_\pi - Q_g] \right] \\ &= \frac{1}{1 - Q_\pi Q_g} \\ &\quad \times \left[\frac{xP - w_\pi + s^{L\pi}K}{r + s^{L\pi} + s^{C\pi} + s^G} \frac{r + s^{Lg} + s^{Cg}}{r + s^{Lg} + s^{Cg} + \lambda} - \frac{s^{Lg}K - w_g}{r + s^{Lg} + s^{Cg} + \lambda} \frac{r + s^{L\pi} + s^{C\pi}}{r + s^{L\pi} + s^{C\pi} + s^G} \right]. \end{aligned}$$

Note that

$$\begin{aligned} \frac{1}{1 - Q_\pi Q_g} &= \frac{1}{1 - \frac{\lambda}{r + s^{Lg} + s^{Cg} + \lambda} \frac{s^G}{r + s^{L\pi} + s^{C\pi} + s^G}} \\ &= \frac{(r + s^{Lg} + s^{Cg} + \lambda)(r + s^{L\pi} + s^{C\pi} + s^G)}{(r + s^{Lg} + s^{Cg} + \lambda)(r + s^{L\pi} + s^{C\pi} + s^G) - \lambda s^G} \\ &= \frac{(r + s^{Lg} + s^{Cg} + \lambda)(r + s^{L\pi} + s^{C\pi} + s^G)}{(r + s^{Lg} + s^{Cg})(r + s^{L\pi} + s^{C\pi}) + (r + s^{Lg} + s^{Cg})s^G + (r + s^{L\pi} + s^{C\pi})\lambda} \end{aligned}$$

implying

$$J_\pi - J_g = \frac{(xP - w_\pi + s^{L\pi}K)(r + s^{Lg} + s^{Cg}) - (s^{Lg}K - w_g)(r + s^{L\pi} + s^{C\pi})}{(r + s^{Lg} + s^{Cg})(r + s^{L\pi} + s^{C\pi}) + (r + s^{Lg} + s^{Cg})s^G + (r + s^{L\pi} + s^{C\pi})\lambda}.$$

Simplifications arise when assuming identical turnover and credit shocks in each stage and finally with equal wages, one has

$$\begin{aligned} J_\pi - J_g &= \frac{(xP - w_\pi + s^L K) - (s^L K - w_g)}{r + s^L + s^C + s^G + \lambda} \\ &= \frac{xP - w_\pi + w_g}{r + s^L + s^C + s^G + \lambda} \\ &= \frac{xP}{r + s^L + s^C + s^G + \lambda}. \end{aligned}$$

The wage equation thus becomes, using the notation $Q'_g = \frac{\lambda}{r + s^L + s^C + s^G + \lambda}$:

$$\begin{aligned} w_g &= (1 - \alpha_L)(rW_u - \bar{y}_0) + \frac{\alpha_L - \alpha_G}{1 - \alpha_G} Q'_g xP - \alpha_L(r + s^{Cg})K \\ &= (1 - \alpha_L)(rW_u - \bar{y}_0) + (\alpha_L - \alpha_G) Q'_g xP - \alpha_L(r + s^{Cg})K. \end{aligned}$$

The price was replaced by its equilibrium expression in the last line. We also have the following simpler cases:

- CLG with $\alpha_L = \alpha_G \Rightarrow w_g = (1 - \alpha_L)(rW_u - \bar{y}_0) - \alpha_L(r + s^{Cg})K$
- LG with $K = 0 \Rightarrow w_g = (1 - \alpha_L)(rW_u - \bar{y}_0) + (\alpha_L - \alpha_G) Q'_g xP$
- CL with $\lambda \rightarrow \infty, \alpha_G = 0 \Rightarrow w_g = (1 - \alpha_L)(rW_u - \bar{y}_0) + \alpha_L[xP - (r + s^{Cg})K]$
- L with $K = 0, \lambda \rightarrow \infty, \alpha_G = 0 \Rightarrow w_g = (1 - \alpha_L)(rW_u - \bar{y}_0) + \alpha_L P_X$.

One can finally use the usual simplification of the value of unemployment to obtain the equations from the text.

$$rW_u = z + \bar{y}^0 + \frac{\alpha_L}{1 - \alpha_L} f(\theta) J_g = z + \bar{y}^0 + \frac{\alpha_L}{1 - \alpha_L} \gamma \theta.$$

Appendix F. Alternative timing for wages and price determination

Assume first that wages are different across states g and π . The goods-market wage is still determined by

$$w_g = \operatorname{argmax} \left((W_{g0} - W_u)^{\alpha_L} (J_g - J_v)^{1 - \alpha_L} \right). \tag{72}$$

In regards to wage w_π , three different timings can be explored (see Brzustowski (2015) for details).

- **Timing 1 (wage w_π negotiated before price):** After w_g is determined, and before having met a customer, the worker and the firm agree on a wage increase $w_\pi - w_g$, which will take effect as soon as the firm starts making profits. The new wage is the outcome of Nash bargaining in anticipation of the later meeting of a customer.
- **Timing 2 (price negotiated before wage w_π):** Instead, this is only once his/her firm has started making profits by having met the customer that the worker renegotiates his/her wage and obtains a bonus $w_\pi - w_g$.
- **Timing 3 (trilateral bargaining over w_π and price):** When a match is formed on the goods market, the customer, the firm's manager, and

the worker of the firm gather and the three of them negotiate together over the price and the new wage.

In what follows, the outcomes of these three timings are presented independently after some preliminary results proved in Brzustowski (2015). Define the surplus of the consumer upon matching with a good:

$$W_{\pi 1} - W_{\pi 0} = W_{g1} - W_{g0} \equiv S_M^W. \tag{73}$$

Notice that Eq. (73) also implies that the surplus gained by the worker of a newly profitable firm does not depend on his/her consumption situation:

$$W_{\pi 1} - W_{g1} = W_{\pi 0} - W_{g0} \equiv S_{\pi}^W. \tag{74}$$

One has:

$$S_M^W = \frac{x(\Phi - \mathcal{P})}{r + s^T + \lambda} \tag{75}$$

$$S_{\pi}^W = \frac{w_{\pi} - w_g}{r + s^T + \lambda}. \tag{76}$$

These expressions are to be compared with the firm's surplus upon matching on the goods market:

$$J_{\pi} - J_g = \frac{x\mathcal{P} - (w_{\pi} - w_g)}{r + s^T + \lambda}. \tag{77}$$

The goods market wage w_g is independent of the future timing of negotiations. Indeed,

$$\begin{aligned} (r + s^C + s^L + \theta q(\theta))(W_{g0} - W_u) &= w_g - z + \lambda(S_M^W + S_{\pi}^W) \\ &= w_g - z + Q'_g[x(\Phi - \mathcal{P}) + (w_{\pi} - w_g)] \end{aligned}$$

and using that $J_v = K(\phi)$, one has:

$$(r + s^C + s^L + \theta q(\theta))(J_g - J_v) = -w_g + \gamma\theta - (1 - \theta)(r + s^C)K(\phi) + Q'_g[x\mathcal{P} - (w_{\pi} - w_g)].$$

As a result, independently of \mathcal{P} and w_{π} , it is always the case that:

$$\frac{\partial(J_g - J_v)}{\partial w_g} = -\frac{\partial(W_{gU} - W_u)}{\partial w_g}.$$

It follows that the simple sharing rule in the main text will always hold:

$$w_g = (1 - \alpha_L)z + \alpha_L(\gamma\theta - (1 - \theta)(r + s^C)K(\phi)) + Q'_g[x\mathcal{P} - (w_{\pi} - w_g) - (1 - \alpha_L)x\Phi]. \tag{78}$$

Timing 1. In this case, the new wage w_{π} is set before the price \mathcal{P} . We denote by α_L^T the bargaining weight of workers in that stage, to distinguish it from the above bargaining weight in stage g α_L . Reason by backward induction and derive first the price. Everything else having already been set, Nash bargaining over the price leads to a simple sharing rule, with α_C the bargaining power of the consumer:

$$(1 - \alpha_C)S_M^W = \alpha_C(J_{\pi} - J_g).$$

Using Eqs. (75) and (77), this yields:

$$\mathcal{P} = (1 - \alpha_C)\Phi + \alpha_C \frac{w_{\pi} - w_g}{x}. \tag{79}$$

Then, the new wage w_{π} can be derived. It is interpreted as an incentive to do a good job, which means that the worker's outside option in the negotiation is to do a "bad" job and let the firm remain in stage g . As a result, the new wage is set as:

$$w_{\pi} = \operatorname{argmax} \left((S_{\pi}^W)^{\alpha_L^T} (J_{\pi} - J_g)^{1 - \alpha_L^T} \right).$$

Taking into account the price rule (Eq. (79)), one has:

$$\frac{\partial(J_{\pi} - J_g)}{\partial w_{\pi}} = -(1 - \alpha_C) \frac{\partial S_{\pi}^W}{\partial w_{\pi}}.$$

Hence

$$\alpha_L^T (J_{\pi} - J_g) = (1 - \alpha_L^T)(1 - \alpha_C)S_{\pi}^W.$$

Finally, one obtains:

$$\alpha_L^T \mathcal{P} = (1 - \alpha_C(1 - \alpha_L^T)) \frac{w_{\pi} - w_g}{x}. \tag{80}$$

The system formed by Eqs. (79) and (80) can be solved to:

$$\frac{w_{\pi} - w_g}{x} = \alpha_L^T \Phi \tag{81}$$

$$\mathcal{P} = (1 - \alpha_C(1 - \alpha_L^T))\Phi. \tag{82}$$

In this case, the goods-market wage w_g has the following expression:

$$w_g = (1 - \alpha_L)z + \alpha_L(\gamma\theta - (1 - \theta)(r + s^C)K(\phi)) + Q'_g(\alpha_L - \alpha_C - \alpha_L^T(1 - \alpha_C))x\Phi. \tag{83}$$

Timing 2. In this case, the new wage w_{π} is set after the price \mathcal{P} . It is assumed for simplicity that the worker's outside option in this negotiation is to make the firm remain in stage g . This corresponds to the case of a strike: the worker refuses to serve the customer as long as (s)he has not gotten a wage increase. It could also be assumed that, rather than going on strike, the worker threatens to resign. However, this would lead to more complicated results. The derivation of the results under timing 2 follows a very similar structure to timing 1 and is left to the reader, who will obtain:

Bonus rule:

$$\frac{w_{\pi} - w_g}{x} = \alpha_L^T \mathcal{P}. \tag{84}$$

Price rule:

$$(1 - \alpha_L^T(1 - \alpha_C))\mathcal{P} = (1 - \alpha_C)(1 - \alpha_L^T)\Phi + \alpha_C \frac{w_{\pi} - w_g}{x}. \tag{85}$$

The system formed by Eqs. (84) and (85) can be solved to:

$$\frac{w_{\pi} - w_g}{x} = (1 - \alpha_C)\alpha_L^T \Phi \tag{86}$$

$$\mathcal{P} = (1 - \alpha_C)\Phi. \tag{87}$$

In this case, the goods-market wage w_g has the following expression:

$$w_g = (1 - \alpha_L)z + \alpha_L(\gamma\theta - (1 - \theta)(r + s^C)K(\phi)) + Q'_g(\alpha_L - \alpha_C - \alpha_L^T(1 - \alpha_C))x\Phi. \tag{88}$$

This is exactly the same expression as in timing 1.

Timing 3. In this case, w_π and \mathcal{P} are set simultaneously as the outcomes of a three-party Nash bargaining:

$$(w_\pi, \mathcal{P}) = \operatorname{argmax} \left[(S_M^W)^{\alpha_G} (S_\pi^W)^{\alpha_L^\pi} (J_\pi - J_g)^{1-\alpha_G-\alpha_L^\pi} \right].$$

The solution couple (w_π, \mathcal{P}) will thus verify:

$$\begin{aligned} (1-\alpha_G-\alpha_L^\pi)S_M^W &= \alpha_G(J_\pi - J_g) \\ (1-\alpha_G-\alpha_L^\pi)S_\pi^W &= \alpha_L^\pi(J_\pi - J_g). \end{aligned}$$

It follows that the bonus-rule/price-rule system takes the form:

$$(1-\alpha_L^\pi)\mathcal{P} = (1-\alpha_G-\alpha_L^\pi)\Phi + \alpha_G \frac{w_\pi - w_g}{x} \tag{89}$$

$$\alpha_L^\pi \mathcal{P} = (1-\alpha_G) \frac{w_\pi - w_g}{x}. \tag{90}$$

This solves to:

$$\frac{w_\pi - w_g}{x} = \alpha_L^\pi \Phi. \tag{91}$$

$$\mathcal{P} = (1-\alpha_G)\Phi. \tag{92}$$

In this case, the goods-market wage w_g has the following expression⁶:

$$w_g = (1-\alpha_L)z + \alpha_L(\gamma\theta - (1-\theta)(r + s^C)K(\phi)) + Q_g(\alpha_L - \alpha_G - \alpha_L^\pi)x\Phi. \tag{93}$$

Appendix G. Calibration Appendix: Source of data

G.1. Credit market parameters

The discount rate r is taken homogenous across countries at 0.0033, which corresponds to an annual 4% rate (U.S. T-bill). Eurostat's *Business demography by size class* [bd_9bd_sz_cl_r2] provides annual data on *Employment share of enterprise deaths for business economy except activities of holding companies*. Dividing the data by 12, we obtain the model's credit separation rate s^C . Eurostat provides data for the period 2008–2011. Given the small variations over that period, s^C is taken constant between 2005 and 2014, equal to the average of the data provided by Eurostat for each country. In the absence of information on the creditor's bargaining power α_C , it is set to 0.5.

Our main target on credit markets is the financial sector's share in GDP, denoted Σ . In the model, the GDP is $\bar{y}^0 + x\mathcal{P}\mathcal{N}_\pi - \gamma\mathcal{V} - \kappa_B\mathcal{B}_c$, and therefore:

$$\Sigma = \frac{\psi\mathcal{N}_\pi - w\mathcal{N}_g - \gamma\mathcal{V} - \kappa_B\mathcal{B}_c}{\bar{y}^0 + x\mathcal{P}\mathcal{N}_\pi - \gamma\mathcal{V} - \kappa_B\mathcal{B}_c}.$$

Data are found in Eurostat's table *National accounts aggregates by industry* [nama_10_a64], from which we take half of the value corresponding to financial activities. That is, we have assumed that credit services to households and to businesses yield tantamount revenues.

Finally, in the absence of further evidence, we target an average six months to find credit for an entrepreneur in 2005. The credit-

matching factor χ_C is then fixed and this target is relaxed for the 2014 calibration. Similarly, it is assumed that the searching costs κ_B and κ_I are equal in 2005; κ_I being then fixed and κ_B relaxed.

G.2. Labor market parameters

We target the unemployment rate \mathcal{U} supplied by Eurostat [une_rt_m] for each country. We follow Shimer (2005)'s method and use Eurostat's *Unemployment by duration of unemployment—quarterly data from the Labour Force Survey* [lfsq_ugad], from which we obtain quarterly values for the short-term unemployment rate (i.e. the rate of unemployed persons who have been unemployed for less than one month), denoted \mathcal{U}^{-1} . Shimer (2005) uses it to estimate the job separation rate, $s^C + s^L$ in our model. Instead, we prefer to estimate a target for the job-finding rate f , and to let s^L be computed by the system. We consider then the rate of persons unemployed for more than one month $\mathcal{U}^{>1} = \mathcal{U} - \mathcal{U}^{-1}$. In the model:

$$\mathcal{U}_t^{>1} = (1-f_{t-1})\mathcal{U}_{t-1}.$$

We have quarterly values for $\mathcal{U}^{>1}$ and monthly values for \mathcal{U} . Hence, values for f at the middle of each quarter can be computed. The annual averages give us a target for f for each year. We target the job vacancy rate \mathcal{V} given by Eurostat's *Job vacancy statistics* [jvs_q_nace2].

We target the share of wages in GDP $\mathcal{W}_{gdp} = \frac{(1-\mathcal{U})w}{\bar{y}^0 + x\mathcal{P}\mathcal{N}_\pi - \gamma\mathcal{V} - \kappa_B\mathcal{B}_c}$ to correspond to the values found in Eurostat's *GDP and main components (output, expenditure, and income)* [namq_10_gdp], which gives quarterly data over 2005–2014 on the *compensation of employees' share*, taking into account *wages and salaries* as well as *employers' social contributions*. Data on unemployment benefit expenditures as a percentage of GDP are provided by Eurostat [spr_exp_gdp] from which we can estimate the ratio z/w for 2005. Unemployment benefits z are then fixed for the 2014 calibration. Finally, we target Silva and Toledo (2009)'s estimation that recruiting costs amount to 3.6% of a monthly wage. The vacancy posting cost γ is then set constant for 2014.

G.3. Goods market parameters

The marginal utility of consuming the frictional good Φ and the pure taste shock rate τ are taken as constant across countries and set as in Petrosky-Nadeau and Wasmer (2015). The quantity of numeraire in the economy \bar{y}^0 is set to 1/12, such that individuals receive one unit of numeraire per year. The rate of capacity utilization is, in the steady-state, equal to:

$$\mu_G(\xi) = \frac{\lambda(\xi)}{s^G + s^{Lg,\pi} + \lambda(\xi)}$$

and the corresponding numbers are provided by Eurostat [ei_bsin_q_r2]. We target the share of the numeraire in total expenditures η taken from Eurostat's *Final consumption expenditure of households by consumption purpose (COICOP 3 digit)* [nama_10_co3_p3]. The numeraire is assumed to correspond to the following categories (COICOP):

- Food and non-alcoholic beverages
- Alcoholic beverages, tobacco, and narcotics
- Water supply and miscellaneous services relating to the dwelling
- Electricity, gas, and other fuels
- Hospital services
- Operation of personal transport equipment
- Transport services
- Postal services
- Education

⁶ Bear in mind that α_C and β_L have been defined differently in this case.

- Personal care
- Social protection

Appendix H. Supplementary data

Supplementary data to this article can be found online at <http://dx.doi.org/10.1016/j.labeco.2016.05.006>.

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